

UCLA

UCLA Previously Published Works

Title

How Accurately Can We Measure the Reconnection Rate E_M for the MMS Diffusion Region Event of 11 July 2017?

Permalink

<https://escholarship.org/uc/item/9z79214b>

Journal

Journal of geophysical research. Space physics, 123(11)

ISSN

2169-9380

Authors

Genestreti, KJ
Nakamura, TKM
Nakamura, R
et al.

Publication Date

2018-11-01

DOI

10.1029/2018ja025711

Peer reviewed



RESEARCH ARTICLE

10.1029/2018JA025711

This article is a companion to
Nakamura et al. (2018)
<https://doi.org/10.1029/2018JA025713>.

Key Points:

- The reconnection rate E_M is estimated for one event using several techniques to find an M direction
- The error bars in E_M and the LMN coordinate directions are estimated from virtual data
- The reconnection rate is likely $E_M = 3.2 \text{ mV/m} \pm 0.6 \text{ mV/m}$, which corresponds to a normalized rate of 0.18 ± 0.035

Correspondence to:

K. J. Genestreti,
kevin.genestreti@oeaw.ac.at

Citation:

Genestreti, K. J., Nakamura, T. K. M., Nakamura, R., Denton, R. E., Torbert, R. B., Burch, J. L., et al. (2018). How accurately can we measure the reconnection rate E_M for the MMS diffusion region event of 11 July 2017?. *Journal of Geophysical Research: Space Physics*, 123, 9130–9149. <https://doi.org/10.1029/2018JA025711>

Received 24 MAY 2018

Accepted 11 SEP 2018

Accepted article online 17 SEP 2018

Published online 10 NOV 2018

How Accurately Can We Measure the Reconnection Rate E_M for the MMS Diffusion Region Event of 11 July 2017?

K. J. Genestreti^{1,2}, T. K. M. Nakamura¹, R. Nakamura¹, R. E. Denton³, R. B. Torbert^{4,5}, J. L. Burch⁵, F. Plaschke¹, S. A. Fuselier^{5,6}, R. E. Ergun⁷, B. L. Giles⁸, and C. T. Russell⁹

¹Space Research Institute, Austrian Academy of Sciences, Graz, Austria, ²Now at Space Science Center, University of New Hampshire, Durham, NH, USA, ³Department of Physics and Astronomy, Dartmouth College, Hanover, NH, USA, ⁴Space Science Center, University of New Hampshire, Durham, NH, USA, ⁵Space Science and Engineering Division, Southwest Research Institute, San Antonio, TX, USA, ⁶Department of Physics and Astronomy, University of Texas at San Antonio, San Antonio, TX, USA, ⁷Laboratory of Atmospheric and Space Sciences, University of Colorado Boulder, Boulder, CO, USA, ⁸Heliophysics Science Division, NASA Goddard Space Flight Center, Greenbelt, MD, USA, ⁹Institute of Geophysics and Planetary Physics, University of California, Los Angeles, CA, USA

Abstract We investigate the accuracy with which the reconnection electric field E_M can be determined from in situ plasma data. We study the magnetotail electron diffusion region observed by National Aeronautics and Space Administration's Magnetospheric Multiscale (MMS) on 11 July 2017 at 22:34 UT and focus on the very large errors in E_M that result from errors in an LMN boundary normal coordinate system. We determine several LMN coordinates for this MMS event using several different methods. We use these M axes to estimate E_M . We find some consensus that the reconnection rate was roughly $E_M = 3.2 \pm 0.6 \text{ mV/m}$, which corresponds to a normalized reconnection rate of 0.18 ± 0.035 . Minimum variance analysis of the electron velocity (MVA- v_e), MVA of E , minimization of Faraday residue, and an adjusted version of the maximum directional derivative of the magnetic field (MDD- B) technique all produce reasonably similar coordinate axes. We use virtual MMS data from a particle-in-cell simulation of this event to estimate the errors in the coordinate axes and reconnection rate associated with MVA- v_e and MDD- B . The L and M directions are most reliably determined by MVA- v_e when the spacecraft observes a clear electron jet reversal. When the magnetic field data have errors as small as 0.5% of the background field strength, the M direction obtained by MDD- B technique may be off by as much as 35°. The normal direction is most accurately obtained by MDD- B . Overall, we find that these techniques were able to identify E_M from the virtual data within error bars $\geq 20\%$.

1. Introduction

1.1. Calculating the Reconnection Rate From In Situ Plasma Data

In situ measurements of the normalized reconnection rate \mathcal{R} have been made at the Earth's magnetopause (Chen et al., 2017; Fuselier et al., 2005; Mozer et al., 2002), its magnetotail (Wygant et al., 2005; Xiao et al., 2007) and its magnetosheath (Phan et al., 2007), in the magnetospheres of other planets such as Mercury (Slavin et al., 2009) and Saturn (Arridge et al., 2016), in the solar wind (Phan et al., 2006), and in laboratory experiments (Egedal et al., 2007). Calculating \mathcal{R} as the rate of change of magnetic connectivity is not possible in practice with in situ space plasma observations, so proxies are typically used that are either directly or with few assumptions equivalent to \mathcal{R} .

In the studies mentioned in the previous paragraph, \mathcal{R} was defined by (1) the upstream inflow speed normalized by the downstream outflow speed $\mathcal{R} = V_{\text{in}}/V_{\text{out}} = v_{Nb}/V_{Aib}$, where v_{Nb} is the inflow speed and V_{Aib} is the ion Alfvén speed in the inflow region, (2) the component of the magnetic field normal to the current sheet normalized by the reconnecting magnetic field strength $\mathcal{R} = B_N/B_b$, where B_b is the strength of the reconnecting component of the magnetic field in the inflow region, (3) the normalized tangential reconnection electric field $E_M/E_b = E_M/V_{Aib}B_b$, or (4) the angle of the ion outflow fan. Here \hat{M} is the direction of the reconnecting current sheet, \hat{N} is the current sheet normal, and $(\pm)\hat{L}$ is the direction of the reconnecting magnetic fields. While the canonical fast reconnection rate is $\mathcal{R} = 0.1$, the exact value of \mathcal{R} may depend on the magnetic shear angle (Fuselier & Lewis, 2011; Mozer & Retinò, 2007), the mass density of minor ion species

©2018. The Authors.

This is an open access article under the terms of the Creative Commons Attribution License, which permits use, distribution and reproduction in any medium, provided the original work is properly cited.

(Liu et al., 2015; S. Wang et al., 2014), the presence of external driving forces (Nakamura et al., 2017), turbulence and anomalous resistivity effects (Che, 2017), etc.

1.2. Effect of Errors in the Measured Coordinate System

The inflow speed v_{Nb} , the normal magnetic field B_N , and the tangential electric field E_M are typically the smallest components of their associated vectors. Very large errors in \mathcal{R} can result from, for example, E_M being evaluated inaccurately as $E_M^* = \vec{E} \cdot \hat{M}^*$, where some measured axis \hat{M}^* has, by error, a finite projection onto the current sheet normal such that $\hat{M}^* = \cos \theta_{NM^*} \hat{M} + \sin \theta_{NM^*} \hat{N}$ and, for sufficiently small θ_{NM^*} , $\mathcal{R}^* \approx (E_M + \theta_{NM^*} E_N)/E_b$. Given that the normal electric field can be tens of times larger than the reconnection electric field (Chen et al., 2017; Mozer & Retinò, 2007; Shay et al., 2016; Torbert et al., 2018), a relatively small error of $\theta_{NM^*} \sim 5^\circ$ could create error bars for \mathcal{R} of $\sim 100\%$. (Note that throughout the rest of the manuscript, the asterisk is used to denote coordinate axes or quantities that are known to be inaccurate).

1.3. Goals of This Study

Here we investigate the accuracy with which we find the normalized reconnection electric field $\mathcal{R} = E_M/E_b$ for a reconnection electron diffusion region (EDR) event observed in the Earth's magnetotail by Magnetospheric Multiscale (MMS) on 11 July 2017 at $\sim 22:34$ UT (Nakamura et al., 2018; Torbert et al., 2018). We focus on the errors in \mathcal{R} that result from inaccuracies in the coordinate system rather than other sources of error that may arise from inaccuracies in the measured electric field, inaccurate determination of the upstream normalization parameter E_b , etc. (see discussion in section 5). While many other techniques exist for estimating \mathcal{R} (see, e.g., our companion paper, Nakamura et al., 2018, hereafter N18), these techniques may have their own unique sources of error that are largely beyond the scope of this study.

In the next sections we discuss the MMS data used in this study (section 2.1), the observations of MMS during the 11 July 2017 EDR event (section 2.2), the setup of the particle-in-cell (PIC) simulation of N18 (section 2.3), and the virtual probe data from the simulation of N18 (section 2.4). In section 3 we find several LMN coordinate systems and reconnection rates from MMS data. In section 4 we apply some of the same analysis techniques to the virtual probe data, where L , M , N , and \mathcal{R} are known and the errors associated with our methods for finding them can be calculated directly. Finally, in section 5, we summarize and discuss our findings.

2. Overview of MMS Data, 11 July 2017 Reconnection Event, and PIC Simulation

2.1. MMS Data

The DC (direct current) magnetic field data are provided by the fluxgate magnetometers at 128 vectors per second during high-time-resolution burst mode and nominally at eight vectors per second (Russell et al., 2016). The spin-plane components ($\sim B_X$ and $\sim B_Y$) of the magnetic field are calibrated to a high degree of accuracy by removing spin tone oscillations in a despun coordinate system. The spin-axis magnetic field component is cross calibrated with data from the electron drift instrument (Torbert et al., 2016). The stated accuracy of the DC magnetic field is ± 0.1 nT. Using data from two quiet magnetotail periods before (22:10–22:20 UT) and after (22:39–22:51 UT) the EDR interval, we found average interprobe differences that were of the order ± 0.05 nT for the spin-axis components, while the absolute differences between the spin-plane components were much smaller on average (~ 0.001 nT) but had small residual spin tones with amplitudes of ~ 0.02 nT.

The coupled AC-DC (alternating current-direct current) electric field data are provided by the electric field double probes instruments at 8,196 vectors per second during burst mode and at 32 vectors per second during fast survey mode (Ergun et al., 2016; Lindqvist et al., 2016). We use the level 3 version of the electric field data, which were determined for this event by Torbert et al. (2018) by cross calibrating $-\vec{v}_e \times \vec{B}$ and \vec{E} to remove offsets in the perpendicular components of \vec{E} (cf. R. Wang et al., 2017). The nominal uncertainty in the perpendicular electric field is expected to be ~ 0.5 mV/m (Torbert et al., 2016).

High-time-resolution plasma ion and electron moments are obtained by the fast plasma investigation suite of sensors (Pollock et al., 2016). In burst mode, 3-D electron (ion) distribution functions and moments are measured once every 30 (150) ms. In regions with very sparse plasma, portions of phase space are undersampled, such that the number of counts per (energy-angle-angle) pixel are comparable to the Poisson uncertainty. This leads to noise in the plasma moments. Other issues related to the data quality of the ion measurements taken during this event are discussed in Torbert et al. (2018).

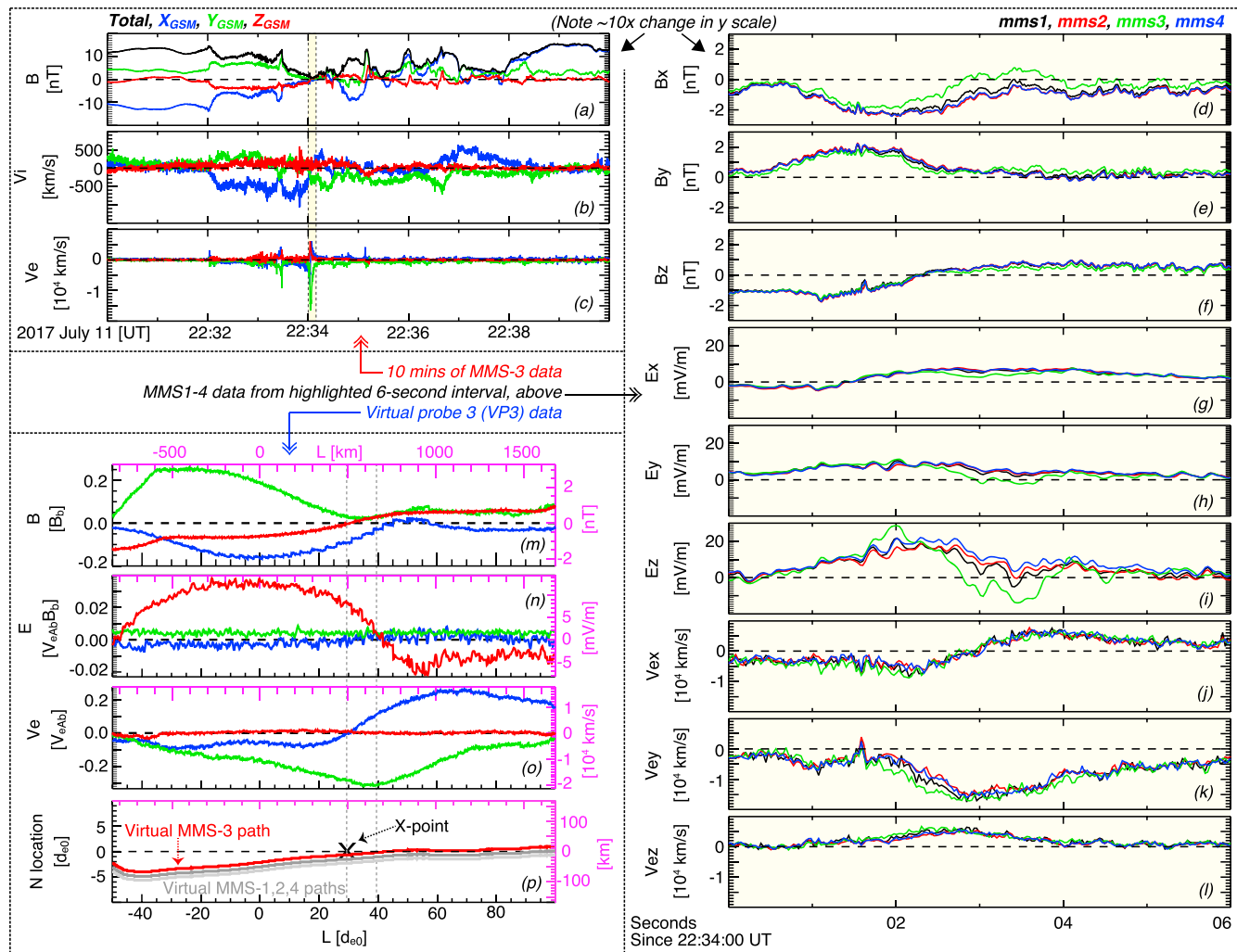


Figure 1. (a) The magnetic field \vec{B} , (b) ion bulk velocity \vec{v}_i , and (c) electron bulk velocity \vec{v}_e from MMS-3 from the roughly 10-min current sheet crossing. The three components of (d)–(f) \vec{B} , (g)–(i) the electric field \vec{E} , and (j)–(l) \vec{v}_e for the roughly 6-s electron diffusion region encounter, which is also indicated in the highlighted region in (a)–(c). (m) \vec{B} , (n) \vec{E} , (o) \vec{B} , and (p) the N - L locations of the orbits of virtual MMS-3 (red), virtual MMS-1 (dark gray), and virtual MMS-2 and 4 (light gray). The vertical black and magenta-colored axes give the quantities in normalized and unnormalized units, respectively. MMS data are shown in geocentric solar magnetospheric coordinates. MMS = Magnetospheric Multiscale.

2.2. Overview of the 11 July 2017 EDR Event

On 11 July 2017 at $\sim 22:34$ UT, MMS observed an EDR in the central magnetotail current sheet. The average interprobe separation was approximately ~ 17 km, which is approximately half of the asymptotic electron inertial length $d_{eb} \approx 30$ km, and the formation was a near regular tetrahedron (tetrahedron quality factor of 0.957; see Figures 2a and 2b; Fuselier et al., 2016). The spacecraft was 22 Earth radii (R_E) geocentric distance, $4 R_E$ duskward of midnight, and less than 50 km ($< 0.007 R_E$) away from the empirical-model-predicted neutral sheet location (Fairfield, 1980), which was the most probable region for MMS to observe the diffusion region during the first magnetotail survey phase (Fuselier et al., 2016; Genestreti et al., 2014). An overview of the data from this event is given in Figure 1, where data from the ~ 10 -min current sheet crossing are in Figures 1a–1c, data from the ~ 6 -s EDR crossing are in Figures 1d–1l, and Figures 1m–1p show the virtual MMS-3 data over a range comparable to Figures 1d–1l. The virtual data will be discussed in section 2.4. Overall, during the 10-min period shown in Figures 1a–1c, the spacecraft moved from the Southern Hemisphere to the Northern Hemisphere (see the negative-to-positive reversal in B_x in Figure 1a) while crossing from the tailward to the earthward pointing reconnection exhausts (see the multiple bipolar variations in B_z with associated $|B|$ enhancements, for example, at 22:36:00 and 22:36:40 UT, in Figure 1b). Several ion-scale flux ropes are observed between the prolonged interval of tailward ion jetting and the prolonged interval of earthward

Table 1
Selected Normalization Parameters for PIC Simulation of N18

Parameter	Value
n_0 (n_b)	0.09 cm^{-3} (0.03 cm^{-3})
d_{e0} (d_{eb})	17.7 km (30.7 km)
B_b	12 nT
B_G/B_b	0.03
$E_b = V_{Aib}B_b$	18.12 mV/m
V_{Aib}	1,510 km/s

jetting (see the negative-to-positive reversal in v_{ix} in Figure 1a; Stawarz et al., 2018), some with intense electric fields, intense currents, and nonideal energy conversion $\vec{J} \cdot \vec{E} \neq 0$ (Zenitani et al., 2011; not pictured). Primarily two of the quadrupolar Hall magnetic field ($\approx B_Y(X, Z)$) regions are observed, as well as both regions of the bipolar normal field ($\approx B_Z(X)$) and reconnecting field ($\approx B_X(Z)$). In the downstream separatrix (near $\sim 22:33:20$ UT), intense parallel electron currents are observed along with intense electric fields and electron heating. In summary, the magnetic field observed during the 10-min crossing is not that of a uniform 1-D current sheet, which is a common assumption of many techniques for finding LMN coordinates.

Parameters describing the initial state of the plasma sheet and lobes were detailed in N18. The plasma sheet ion and electron densities and temperatures were selected in the interval between 22:32 and 22:33 UT. The plasma sheet density was determined to be $n_0 \approx 0.08\text{--}0.1 \text{ cm}^{-3}$, and the ion temperature was $T_{i0} \approx 4,000\text{--}5,000$ eV. The lobe densities and temperatures were determined near the EDR interval and near 22:33:30 during two brief excursions outside the reconnection separatrices. These lobe values were $T_{ib} \approx 1,000\text{--}2,000$ eV and $n_b \approx 0.03 \text{ cm}^{-3}$. The electron temperatures were roughly one third of the ion temperatures. The lobe magnetic field was roughly $B_b \approx 10\text{--}12$ nT. The variability and uncertainty in these parameters indicate that $E_b = V_{Aib}B_b$, the parameter that normalizes the reconnection rate $\mathcal{R} = E_M/E_b$, may not have been determined perfectly accurately. However, the best estimate for this parameter is $E_b = 18.12$ mV/m, using the average values for the upstream Alfvén speed V_{Aib} and lobe magnetic field. The combined pressures derived from these lobe values are roughly in balance with the combined pressures determined from the plasma sheet thermal pressure (see N18).

Torbert et al. (2018) analyzed multiprobe data, including electron velocity distribution functions, and concluded that this event was consistent with simulations of laminar 2-D reconnection. N18 compared 2.5 and 3-D simulations of this reconnection event and found that near the EDR, the two simulations were nearly identical. We have determined the magnetic field dimensionality parameters of Rezeau et al. (2018) for this event and find that they support this conclusion of Torbert et al. (2018) and N18. Rezeau et al. (2018) defined parameters $D_1 \equiv (\lambda_1 - \lambda_2)/\lambda_1$, $D_2 \equiv (\lambda_2 - \lambda_3)/\lambda_1$, and $D_3 \equiv \lambda_3/\lambda_1$, where λ_1 , λ_2 , and λ_3 are the eigenvalues of the time-dependent, 3-D, symmetric matrix $\nabla \vec{B}(\nabla \vec{B})^T$ (Shi et al., 2005), $\lambda_1 \geq \lambda_2 \geq \lambda_3$, and $D_1 + D_2 + D_3 = 1$. D_3 , which is associated three-dimensional structure, was very small as λ_3 was within the uncertainty in $\nabla \vec{B} \nabla \vec{B}^T$ ($\leq 10^{-5} \text{ nT}^2/\text{km}^2$). On average, throughout the EDR, we found that $D_1 \approx 90\text{--}97\%$ and $D_2 \approx 3\text{--}10\%$, implying that (1) the magnetic field gradients were much stronger in the N direction than in L and that (2) any gradients in the out-of-plane direction were too small to be resolved.

During the ~ 6 -s EDR crossing (22:34:00–22:34:06 UT), MMS moved mostly laterally through the EDR in the L direction while largely remaining southward of the current sheet center. Between 22:34:01 and 22:34:02 UT the spacecraft exited the electron current layer and crossed the separatrix into the inflow region (see magnetic field profile in Figures 1d–1f and Torbert et al., 2018). The current sheet moved southward and the spacecraft reentered the EDR between 22:34:02 and 22:34:03 UT. The B_Z reversal (Figure 1f), which corresponds roughly to the crossing of the reconnection midplane, occurred between 22:34:02 and 22:34:03 UT at approximately the same time as the reversal of the electron jets (Figure 1j). A small ~ 2 -nT Hall magnetic field was observed between 22:34:01 and 22:34:02.5 UT (Figure 1e), when the spacecraft were southward of the central electron current layer and tailward of the reconnection midplane. An intense (≤ 30 mV/m) northward Hall electric field (Figure 1i) was observed by all four spacecraft throughout the EDR encounter. MMS-3, which was the only spacecraft that crossed northward of the current sheet for a significant amount of time (1–2 s), observed a reversal in the Hall electric field.

2.3. PIC Simulation Setup

We analyze the 2.5-dimensional PIC simulation of our companion paper, N18, which used the initial conditions listed in Table 1 (e.g., an initial plasma sheet density of $n_0 = 0.09 \text{ cm}^{-3}$ and an initial background lobe density of $n_0 = 0.03 \text{ cm}^{-3}$) to define the initial conditions of their 1-D Harris current sheet with a weak guide field ($B_G = 0.03B_b$). The strength of the guide field was chosen based on the value of B_M during crossings of the current sheet near the EDR, where B_M was determined in the LMN coordinate system based on minimum variance analysis of the electron velocity (MVA- v_e), as is discussed later. The simulation was created with the VPIC code (Bowers et al., 2008, 2009). The ion-to-electron mass ratio was 400, the system size was $120d_{i0} \times$

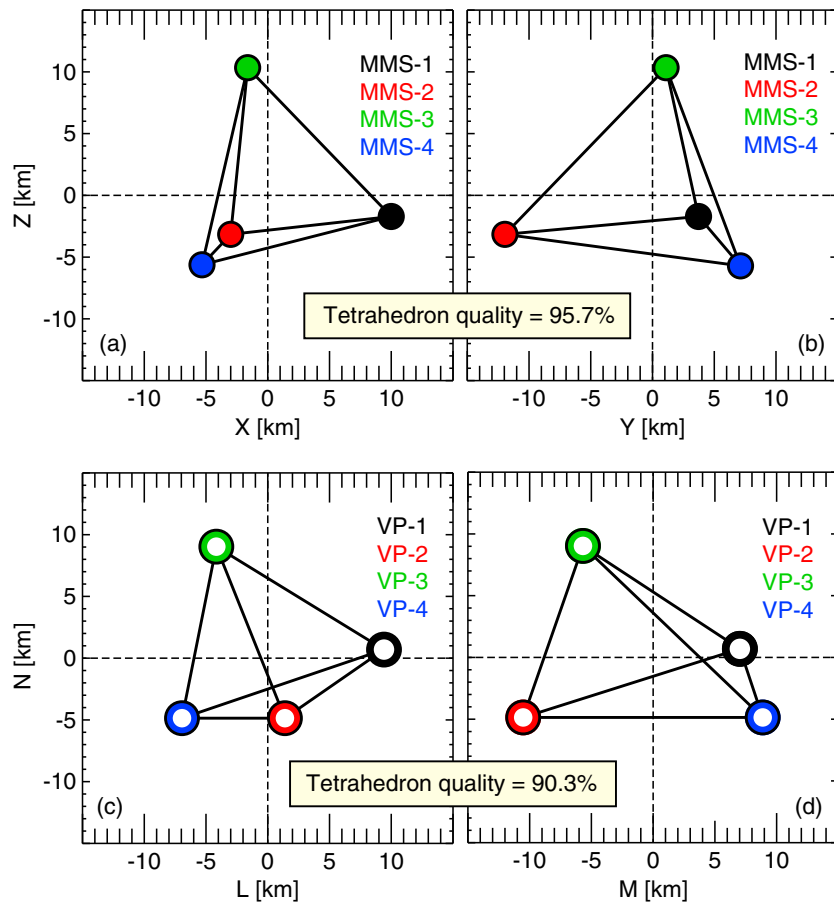


Figure 2. The configuration of the MMS tetrahedron in the (a) X - Z_{GSM} and (b) Y - Z_{GSM} planes. The configuration of the virtual tetrahedron in the (c) L - N and (d) M - N planes. The tetrahedron quality factor is primarily based on the difference in volume between the actual tetrahedron and a regular tetrahedron with axes of the length of the average interprobe distance (Fuselier et al., 2016). MMS = Magnetospheric Multiscale.

$40d_{i0}$ (d_{i0} is the ion inertial length of the initial plasma sheet), and a total of 1.4×10^{11} superparticles was used. The boundaries along the L direction were periodic, and the boundaries along the N direction were conducting walls. Reconnection was initiated from a weak magnetic perturbation, as described in N18. As in N18, we analyze the simulation output from a single point in time 50 ion cyclotron periods after the start of the simulation ($t = 50\Omega_{ci0}$) when reconnection was proceeding near the EDR in a steady state.

For a more detailed description of the simulation setup and choice of virtual probe path, the reader is directed to N18. In their study, N18 also determined the normalized reconnection rate \mathcal{R} of their simulation by evaluating the strength of the reconnection electric field at the X-point normalized by $v_{\text{out}}B_b$ and by determining the opening angle of the separatrix (Liu et al., 2017). The normalized rate determined from the electric field was $\mathcal{R} = 0.17$. The normalized rate determined with the method of Liu et al. (2017) was $\mathcal{R} = 0.186$.

2.4. Virtual MMS Data

N18 determined an irregular cut through their simulated 2-D EDR at $t = 50\Omega_{ci0}$. In their paper, they referred to this cut as *orbit 1-s*, the N coordinate of which is given by the red curve in Figure 1p. The L - N location was optimized such that the B_L along the cut matched the B_L observed by MMS-3, assuming that the velocity of MMS through the EDR was constant in the L direction. The virtual data along this path, some of which are shown in Figures 1m–1p, reproduced many of the key features of reconnection that were observed by MMS-3 during its flight through the EDR. The small Hall magnetic field during the excursion into the inflow region, the strong and varying Hall electric field, the intense electron jet reversal and out-of-plane electron current, the strength of the normal reconnection magnetic field component, the asymmetry between the

earthward and tailward electron jets, etc., are in reasonably good qualitative and quantitative agreement with the MMS-3 data.

Three other virtual probe paths were created to complete the virtual MMS tetrahedron, which were based on the path of the virtual MMS-3 orbit and the location of MMS-1, 2, and 4 relative to MMS-3 (see Figure 1p). We then found it necessary to adjust the virtual probe positions to maintain a relatively regular tetrahedron, given that the interspacecraft separation of MMS ($0.5\text{--}0.6d_{e0}$) was on the order of the separation between (discrete) grid cells ($\sim 0.1d_{e0}$). The configurations of the MMS and virtual tetrahedrons are shown in Figures 2a and 2b and in Figures 2c and 2d, respectively. To confirm that the virtual tetrahedron was regular enough to be considered *MMS like*, we compared the current density vectors from the curlometer technique (Chanteur, 1998) and four-point-averaged plasma moments, which had a very high correlation ($R = 0.993$) similar to that of MMS ($R = 0.990$). The similarity of the virtual and actual tetrahedrons ensures that the errors resulting from the assumption of linear gradients during multipoint analysis should also be similar.

3. Finding *LMN* and *R* With MMS Data

3.1. Defining the Coordinate Systems

We have identified 14 *LMN* coordinate systems for the 11 July 2017 EDR event using a number of different techniques, which range from the overly simple to the extremely sophisticated. The axes of the 14 coordinate systems are shown in Figure 3. The coordinate axes are also tabulated in Appendix A. In general, *L* is mostly along X_{GSE} , *M* is along Y_{GSE} , and *N* is along Z_{GSE} . The average angular separation between *L* axes is $16^\circ \pm 11^\circ$, the average separation between *M* axes is $19^\circ \pm 11^\circ$, and for *N*, the average separation is $13^\circ \pm 7^\circ$.

3.1.1. Simple Coordinates

Our first two coordinate systems are not based on MMS data and are likely overly simple. We use solar-wind-aberrated GSM (GSW) coordinates (cf. Fairfield, 1980), where $L = X_{GSW}$, $M = Y_{GSW}$, and $N = Z_{GSW}$.

We define another *LMN* system with the empirical neutral sheet model of Fairfield (1980), where $L = X_{GSW}$, *M* is the normalized projection of Y_{GSW} onto the current sheet surface and is perpendicular to *L*, and *N* is the modeled current sheet normal.

3.1.2. MVA Coordinates

The remaining coordinate systems are determined with MMS data. The following techniques define *L*, *M*, and *N* as the vector solutions to an eigenvalue problem. To identify the *best quality* coordinate system, we first select a time period over which to apply a technique. We then adjust the time period such that the eigenvalues λ_L , λ_M , and λ_N are well separated. The coordinate axes should also be relatively stable when the time period is altered slightly.

We define two *LMN* coordinate systems for the 11 July 2017 event using minimum variance analysis of the magnetic field (MVA-B; Sonnerup & Cahill, 1967). First, we apply MVA-B to a long-duration current sheet crossing ($\sim 22:05\text{--}22:55$ UT), excluding intervals where flux ropes, a moderate-strength and varying Hall magnetic field, and a weak but varying reconnection magnetic field were observed, that is, where the current sheet is clearly not 1-D (see section 2.2 and Figures 1a–1c). Since we exclude the interval containing the reconnection site, this technique assumes that the current sheet orientation did not change significantly in time. It also assumes that the configuration of the EDR (at the time when it observed) is identical to the average long-time-scale configuration of the current sheet.

MVA-B is also applied over a shorter time scale crossing of the current sheet near the EDR ($\sim 22:30\text{--}22:40$ UT). By reducing the time span over which MVA-B is applied, any errors in the coordinate system caused by temporal or spatial variations in the current sheet orientation should be mitigated. However, since all three components of the magnetic field are expected to vary over this time interval (unlike a 1-D current sheet), the eigenvector system of the variance matrix may not represent the actual natural coordinate system of the current sheet and reconnection site.

We define two more *LMN* coordinate systems using MVA-E (Paschmann et al., 1986; Sonnerup, 1987). MVA-E defines the *N* and *M* directions as the maximum and minimum variance directions of \vec{E} , respectively. The first coordinate system is found by applying MVA-E to the entire reconnection site interval centered on the EDR ($\sim 22:32\text{--}22:45$ UT), wherein the spacecraft entered the ion-scale current sheet from the southern inflow region before exiting back into the southern inflow region. The *L* and *M* coordinate axes were apparently not well resolved at this time scale (i.e., λ_L/λ_M was never much larger than 1). This is possibly due to the large electric fields in the separatrix region observed during the current sheet crossing, errors in the current sheet

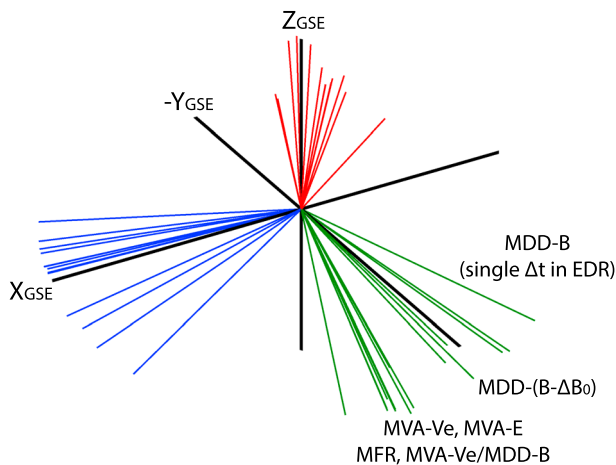


Figure 3. The *LMN* axes of all coordinate systems, where *L* axes are colored blue, *M* axes are green, and *N* axes are red. MDD = maximum directional derivative; EDR = electron diffusion region; MVA = minimum variance analysis; MFR = minimization of Faraday residue.

velocity frame (which was assumed to be constant), time dependence effects or interactions between the reconnection site and the downstream system that lead to variations in the reconnection electric field E_M , etc. A better coordinate system may be defined using the joint variance technique of Mozer and Retinò (2007), where MVA-E is used to identify *N* and then MVA-B is used to identify *L*.

Another coordinate system is defined by applying MVA-E to data from within the EDR (22:34:00.7–22:34:03.9 UT). Here the amplitude of the bipolar E_N is extremely large and reversals of E_N are observed with each partial current sheet crossing (Figure 1i). Also, in the EDR, there is a moderate E_L that reverses its polarity near the B_N reversal (Figures 1g and 1f). Finally, since only a short time span around the central EDR is considered, it is likely more reasonable to assume that the reconnection electric field E_M should vary minimally here. Unlike the previous MVA-E coordinate system, λ_L/λ_M was large (≈ 32.7) and λ_N/λ_L was poor (≈ 2.9). For other time intervals within the EDR, both λ_L/λ_M and λ_N/λ_L were moderate. Since the focus of this paper is the reconnection rate E_M , however, we chose to maximize the quality of *M*.

Two more *LMN* coordinate systems are defined by applying MVA to the ion and electron bulk velocities, MVA- v_i and MVA- v_e , respectively. For both of these coordinate systems, it is assumed that *L* is the jet reversal and thus the maximum variance direction, *N* is the inflow direction and thus the minimum variance direction, and *M* is the intermediate variance direction. The MVA- v_i -based coordinate system was determined over the ion jet reversal period and was reasonably stable. However, the eigenvalue resolution was poor ($\lambda_L/\lambda_M \approx 4$ and $\lambda_M/\lambda_N \approx 6$) and the coordinate system did not organize the data near the EDR. This may be due to the quality of the ion moments data (see discussion in Torbert et al., 2018) or possibly due to asymmetries in the jets and/or nonuniform cross-tail current structure.

Another coordinate system was determined by applying MVA- v_e to MMS-3 data from the electron jet reversal period in the central EDR (22:34:02–22:34:04 UT). Again, the eigenvalue resolution was poor ($\lambda_L/\lambda_M = 4.4$ and $\lambda_M/\lambda_N = 14$), though the resulting coordinate system seemed to do a very good job at organizing the data in and around the EDR (see discussion and Figures 4a–4c in the next section). The poor eigenvalue resolution may be due to the considerable amount of noise in v_e , which might affect MVA by adding unphysical variance. Our possibly naive attempts to filter out the noise (boxcar averaging, smoothing, etc.) moderately improved the eigenvalue separation but appeared to reduce the quality of the coordinate system (one example being that the reconnection electric field became time varying, at times unrealistically large or strongly negative). We also note that the eigenvalue separation and coordinate system quality was reduced when MVA- v_e was applied to the three spacecraft that were further from the current sheet center. This point will be examined in section 4 with virtual data from our simulation. Lastly, we note that since the density across the EDR is almost constant (excepting noise) and $v_i \ll v_e$, MVA- v_e is essentially identical to MVA-*J*.

3.1.3. Minimization of Faraday Residue Coordinates

Another *LMN* coordinate system is defined with the minimization of Faraday residue (MFR) technique (Khrabrov & Sonnerup, 1998). In MFR, the coordinate axes are found from time series data of \vec{E} and \vec{B} from a single spacecraft and are coupled to the velocity of the boundary layer along its normal. We found that the coordinate axes were unstable when changes were made to the time interval over which MFR was applied, possibly due to the irregular and time-dependent EDR motion (see predicted path of MMS in Figure 1p) and/or the complex structure of the current sheet at the EDR (Sonnerup et al., 2006). However, the eigenvalue separation reached a clear maximum for the period between 22:34:02 and 22:34:03.5 UT ($\lambda_L/\lambda_M = 6.2$ and $\lambda_M/\lambda_N = 50.1$). The MFR normal velocity of the current sheet was $u_N = 86.6$ km/s, which is reasonably close to the normal velocity of ~ 70 km/s that was obtained by Torbert et al. (2018) via timing analysis of the B_N reversal. We have also applied the method of Sonnerup and Hasegawa (2005), which is essentially a generalization of MFR for a 2-D boundary layer. We do not find any period near the EDR over which this method returns sensible and stable results, which may be due to the irregular motion of the EDR.

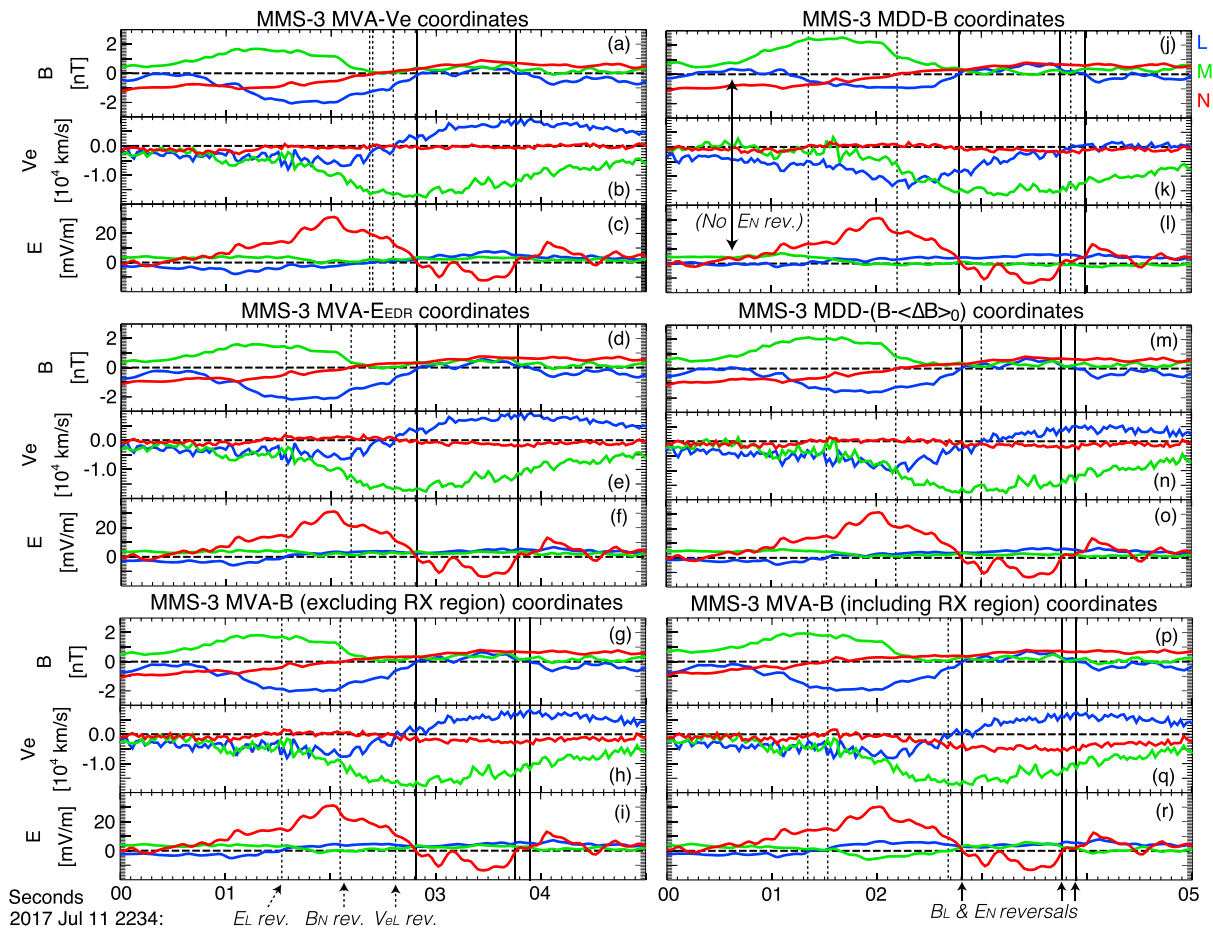


Figure 4. MMS-3 data, which are shown in the LMN coordinates that were determined by (a–c) applying MVA- v_e to data from 22:34:02 to 22:34:04 UT, (d–f) applying MVA- E to data from 22:34:00.7–22:34:03.9 UT, (g–i) applying MVA- B to data from the interval $\sim 22:05$ –22:55 UT (excluding the reconnection region around $\sim 22:30$ –22:40 UT where the current sheet is clearly not 1-D), (j–l) applying MDD- B to data from 22:34:02 to 22:34:04 UT, (m–o) applying MDD- $(B - \Delta B_0)$ to data from different time periods in which L , M , and N are individually stable and subtracting the average magnetic field gradient determined over a quiet interval before finding the MDD- B matrix, and (p–r) applying MVA- B to data from the interval $\sim 22:30$ –22:40 UT. The vertical dashed lines mark the reversals of E_L , B_N , and v_{eL} , which should be aligned in time according to our model. The vertical solid lines mark the reversals of B_L and E_N , which were observed after the midplane crossing. MVA = minimum variance analysis; MMS = Magnetospheric Multiscale; MDD = maximum directional derivative.

3.1.4. Maximum Directional Derivative of B Coordinates

Lastly, we define a group of LMN coordinate systems based on the maximum directional derivative of \vec{B} (MDD- B) technique of Shi et al. (2005). This technique can be used to find a coordinate system for every point in time where four-point measurements of \vec{B} are made. The logic is as follows: N is the direction along which the gradient of \vec{B} is maximized, M is the invariant direction of \vec{B} , and L is the intermediate gradient direction. A time-varying LMN coordinate system is then defined by the eigenvectors of the symmetric, time-dependent 3×3 matrix $\nabla \vec{B}(t)(\nabla \vec{B}(t))^T$. An average coordinate system can be defined by finding the eigenvectors of $\langle \nabla \vec{B}(t)(\nabla \vec{B}(t))^T \rangle$ after averaging the matrix over some period of time where the time-varying axes are stable. The measured electron velocities (Figures 1j–1l) and current densities are very similar for all four spacecraft, which implies that the magnetic field likely varies linearly within the spacecraft tetrahedron.

First, we find L , M , and N simultaneously by applying MDD- B to data from the period between 22:34:02 and 22:34:03.1 UT. The ratio of the N and M eigenvalues is large ($\lambda_N/\lambda_M = 752$), but the data are most likely very poorly organized by the resulting coordinate system, as will be discussed in section 3.2.

Next, we define a coordinate by applying MDD- B to two different periods, one for which M is stable and well resolved (22:34:01.6–22:34:03.1 UT) and then another for which N is stable and well resolved (22:34:02.3–22:34:04 UT). The N axis is then adjusted to be perpendicular to M . The L axis is defined by their cross product.

We define yet another coordinate system where the intercalibration of the four-point measurements of \vec{B} is adjusted before applying MDD- B . We first calculate the average differences between the four-probe magnetic field vectors $\langle \Delta \vec{B} \rangle_0$ over a quiet 2-min period (22:49–22:51 UT). In this quiet interval, the curlometer current was much larger than the current detected by the plasma instruments, implying that the gradients in \vec{B} should be largely unphysical. We find that the average values of $\langle \Delta \vec{B} \rangle_0$ for each vector component for each spacecraft are smaller than ~ 0.05 nT, which is well within the reported error for the magnetometer data (see section 2.1). We also find that subtracting $\langle \Delta \vec{B} \rangle_0$ from \vec{B} reduces the value of the linear approximation of $\nabla \cdot \vec{B}$ in the interval around the EDR. ($\nabla \cdot \vec{B}$ is commonly associated with the error in the linear gradient technique, though, in this case, it is likely associated with small errors in the intercalibration of the magnetometers). There is still an apparent residual spin tone of $\sim \pm 0.02$ nT in the spin-plane components of \vec{B} , but we get poor results from fitting and extrapolating this spin tone beyond the quiet time interval. The adjusted MDD- B coordinate system (referred to as MDD- $(B - \Delta B_0)$) is defined in an almost identical manner to the last coordinate system, though the MDD- B matrix is found by $\nabla(\vec{B} - \langle \Delta \vec{B} \rangle_0)(\nabla(\vec{B} - \langle \Delta \vec{B} \rangle_0))^T$. This technique is similar to the *perturbed MDD- B* technique of Denton et al. (2010, 2012). While this method is expected to account for constant errors in \vec{B} , it does not account for the time-dependent spin tone in the spin-plane components of \vec{B} .

3.1.5. Hybrid Coordinate Systems

The final two coordinate systems are based on hybrid techniques, where N is determined from MDD- B and the other directions are determined separately. Similar coordinate systems were determined with MMS data by Denton et al. (2018). One coordinate system is from Torbert et al. (2018), which applied MDD- B to data at the B_z reversal to determine N , used the maximum component of the time-averaged current to determine M , and then found L to complete the right-handed coordinate system.

For our final coordinate system, L was defined with MVA- v_e , M was defined as the cross product of L and the normal from MDD- B , and N completed the right-handed system.

Other multiprobe techniques for finding the normal direction, for example, constant velocity or timing analysis (Haaland et al., 2004) and local normal analysis (Rezeau et al., 2018), may be used to find additional hybrid LMN coordinate systems. These techniques were also applied to the 11 July 2017 event; however, issues related to the data quality and/or crossing geometry prevented these techniques from producing reasonable normal directions.

3.1.6. Summary of 14 LMN Coordinate Systems

In summary, 14 coordinate systems are found by the following:

1. Using GSW coordinates,
2. Using modified GSW coordinates fixed to the Fairfield (1980) neutral sheet model,
3. Applying MVA- B to data from a long-duration current sheet crossing, excluding the reconnection region,
4. Applying MVA- B over the reconnection region,
5. Applying MVA- E over a long time interval with a current sheet crossing,
6. Applying MVA- E over a short time interval surrounding the EDR,
7. Applying MVA- v_i over the ion jet reversal,
8. Applying MVA- v_e over the electron jet reversal,
9. Applying MFR within the EDR, over a period where the normal velocity appeared to be steady,
10. Applying MDD- B over one time period,
11. Applying MDD- B over two time periods (one to find M then another to find N and thus L),
12. Applying MDD- $(B - \Delta B_0)$ over the same two time periods after subtracting the small average interprobe differences $\langle \Delta \vec{B} \rangle_0$ from each of the four measurements of \vec{B} ,
13. Defining M as the maximum direction of the current density in the EDR, applying MDD- B near the X-point to find N perpendicular to M , and defining L perpendicular to M and N (see Torbert et al., 2018), and finally
14. Defining L with MVA- v_e , defining M as the cross product of L and the MDD- B normal, and finding N perpendicular to L and M .

3.2. The EDR Structure in Different Coordinate Systems

Figure 4 shows \vec{B} , \vec{v}_e , and \vec{E} data from MMS-3 during the EDR observation. The data are shown in six different coordinate systems, which are listed in the figure caption. We compare the data in these coordinate systems to what would be expected for a simple picture of 2-D, steady state, laminar, and symmetric reconnection,

which seems to be a reasonable approximation for this event, as is discussed in section 2.2 and N18. The vertical dashed lines mark the reversals of B_N , v_{eL} , and E_L , which are expected signatures of a crossing of the reconnection midplane. These signatures are expected to be simultaneous for the simple reconnection picture. The solid vertical lines mark the major reversals of B_L and E_N , which are signatures of a neutral sheet crossing. Away from the neutral sheet, E_N and B_L should be oppositely signed for antiparallel reconnection; however, as is shown by our virtual data in Figures 1m and 1n, like signs of E_N and B_L (and B_N) may occur with even a very small guide field. Specifically, for a small positive guide field, E_N may be negative tailward and immediately southward of the neutral sheet (i.e., E_N , B_N , and B_L are all small and negative), whereas E_N may be positive earthward and immediately northward of the neutral sheet (i.e., E_N , B_N , and B_L are all small and positive). This is also shown in Figure 6 of our companion paper, N18. Also, in the simple reconnection picture, the reconnection electric field E_M should be uniform and positive around the diffusion region, given E_M is responsible for the steady circulation and change of connectivity of flux tubes in the EDR. Lastly, the normal electron bulk velocity v_{eN} should be very small or 0 at the neutral sheet where ($B_L = 0$), given that the momenta of two symmetric inflow regions balance one another at the current sheet center.

As is evident in Figures 4a–4f, the data in the MVA- v_e and MVA- E coordinate systems look very similar. The most pronounced crossing of the neutral sheet occurs between 22:34:02.8 and 22:34:03.8 UT and has nearly simultaneous reversals in E_N and B_L . The guide field, as defined by the strength of B_M at the X-point, is ~ 0.3 – 0.4 nT for both coordinate systems. E_M is relatively constant, small, and positive in both coordinate systems. This condition is used to define the MVA- E coordinate system, but it is not considered during MVA- v_e . In the MVA- v_e coordinate system, the reversals of B_N , v_{eL} , and E_L occur within a quarter of a second. For the MVA- E coordinate system, wherein the quality of M was preferred over N and L , these reversals are observed within roughly one second of each other. Lastly, we note that v_{eN} is either very small or 0 at neutral sheet in both the MVA- v_e and MVA- E coordinate systems. This is a condition used to define the MVA- v_e coordinate system, but it is not considered during MVA- E . (Though this is not pictured here, the MFR and hybrid MVA- v_e /MDD- B coordinate systems are quite similar to the MVA- E and MVA- v_e coordinate systems).

The MDD- B coordinate system, in which the data in Figures 4g–4i are shown, is quite different from the MVA- v_e and MVA- E systems, as is also shown in Figure 3. The electron jet is highly asymmetric. The earthward jet is barely visible above the noise. The reversals in B_N , v_{eL} , and E_L are separated from one another by 2.5 s (compared to < 0.25 s for MVA- v_e and < 1 s for MVA- E). Nearly simultaneous reversals in B_L and E_N are observed after the B_N reversal, but there is a nearly 1-s reversal of B_L around 22:34:00.5 UT that is not associated with any significant reversal in E_N . The signs of B_L , B_N , and E_N here do not match our picture of weak guide field $B_M > 0$ reconnection. The guide field strength estimated in these coordinates is $B_G > 1$ nT, which is significantly larger than previously expected but still small compared to the $B_b = 12$ -nT background field. Lastly, the reconnection electric field is not constant and often negative. The MDD- $(B - \Delta B_0)$ coordinate system (Figures 4j–4l) compares much more favorably with the simple reconnection picture and with the data in the MVA- v_e and MVA- E coordinate systems. For instance, the subtraction of ΔB_0 (1) reduces the time between the v_{eL} , B_N , and E_L reversals by a factor of 2.5, (2) leads to E_M remaining small, relatively constant, and positive, (3) enhances the asymmetry in E_L in a manner that matches our virtual data, (4) reduces the asymmetry in v_{eL} in a manner that matches our virtual data, (5) reduces the guide field strength to $B_G \approx 0.5$ nT, which is comparable to its determined value with MVA- v_e coordinates, etc. The L , M , and N axes of the MDD- $(B - \Delta B_0)$ systems are separated by 21° , 21° , and 2° from the corresponding axes of the original MDD- B system.

Lastly, we consider MVA- B . Both of our MVA- B coordinate systems are determined over a much larger time span than any of the others shown in Figure 4, since a full current sheet crossing is required for this technique. Proper identification of L , M , and N by MVA- B requires the current sheet to be roughly 1-D. Since the time spans for these coordinate systems are much longer duration than the EDR encounter, the resulting LMN coordinates are only relevant to the EDR interval if the current sheet orientation does not change in time. Neither coordinate system matches each of the criteria laid out previously for simple 2-D, laminar, symmetric, and steady state reconnection, though the coordinate system in Figures 4g–4i (where MVA- B is applied to a longer duration current sheet crossing and the reconnection region interval is excluded) arguably comes closer to doing so than the coordinate system in Figures 4p–4r. This claim is based on the larger v_{eN} in Figure 4q, the longer interval of more strongly negative E_M in Figure 4r, the greater separation between the reversals of B_N , E_L , and v_{eL} in Figures 4p–4r, etc. Similar to the MDD- B coordinates, we take this as an indication that a more educated

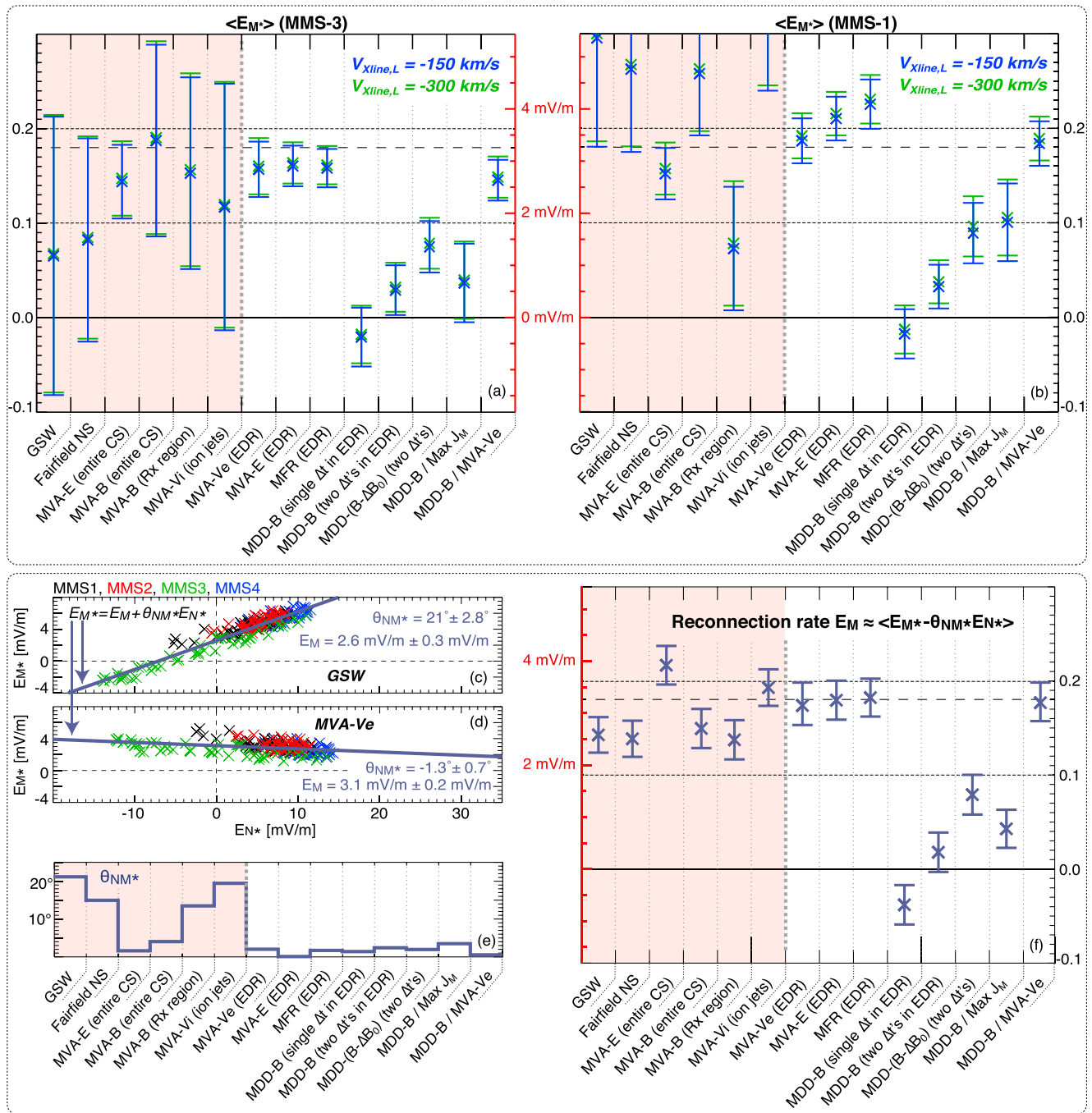


Figure 5. (a and b) The reconnection rate E_M in the X-line frame determined from MMS-3 (left column) and MMS-1 (right column) for each of the 14 LMN coordinate systems. The crosses (X) mark the averaged E_M determined over the period 22:34:03–22:34:04 UT. The error bars mark $\pm \sigma_{E_M}$, the standard deviation of the reconnection rate over this period. The blue crosses (X) mark the reconnection rates determined in the X-line frame of Torbert et al. (2018), and the green crosses (X) are determined in a frame moving twice as fast. The reconnection rate determined from the MMS data at the near-EDR separatrix by N18 is marked by the long dashed horizontal line ($R = 0.18$). The range for the reconnection rate determined by Torbert et al. (2018) is between the two horizontal dotted lines ($0.1 \leq R \leq 0.2$). The data in the red-shaded region are determined using coordinate systems that are not solely based on MMS data from within the EDR. MMS = Magnetospheric Multiscale; EDR = electron diffusion region; GSW = solar-wind-aberrated geocentric solar magnetospheric; MVA = minimum variance analysis; MDD = maximum directional derivative; MFR = minimization of Faraday residue.

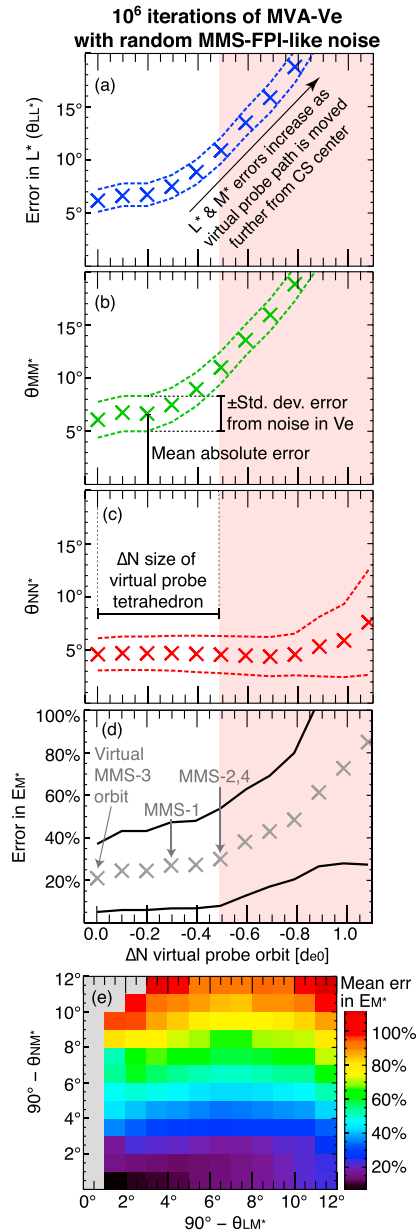


Figure 6. Errors in the coordinate axes and reconnection rate determined by applying MVA to the virtual electron bulk velocity v_e after random MMS-like noise was added. (a)–(d) show these errors as a function of the distance of our MMS-like virtual probe path from its initial location near the current sheet. The crosses (X) indicate the average errors from 10^6 iterations. The dashed lines are the average values plus or minus a standard deviation. The vertical axes are (a) the error in the measured L^* axis, $\theta_{LL^*} \equiv \cos^{-1}(\hat{L} \cdot \hat{L}^*)$, (b) θ_{MM^*} , (c) θ_{NN^*} , and (d) the percent error in E_{M^*} . The red-shaded box indicates the region where the displacement in the virtual probe orbit is larger than the tetrahedron size. (e) The degree of nonorthogonality between L and M^* ($90^\circ - \theta_{LM^*}$) on its horizontal axis, $90^\circ - \theta_{NM^*}$ on the vertical, and the mean error in the reconnection rate per $1^\circ \times 1^\circ$ bin in color. MMS = Magnetospheric Multiscale; MVA = minimum variance analysis; FPI = fast plasma investigation.

not likely to be the cause for the large differences between the two values of E_M in, for example, MVA- v_e or GSW coordinates. We also note that the $-\vec{V} \times \vec{B}$ electric field due to the relative motion of the X-line and the spacecraft was a negligible source of error for \mathcal{R} , as is demonstrated by the very small differences between

application of a coordinate system technique tends to make the MMS data more closely resemble both the virtual data and the simple reconnection picture.

3.3. Calculating \mathcal{R} With MMS Data

Having identified 14 different LMN coordinate systems, we now find E_M and normalize by $E_b = 18.12$ mV/m (see discussion in section 2 and N18) to obtain \mathcal{R} . The reconnection electric field is determined by averaging E_M over the period from 22:34:03 to 22:34:04 UT, which is the period nearest the B_N reversal where the total electric field is smallest (see section 2.2). Given that the largest value of E_N is observed during the B_N reversal, the interval around the B_N reversal is not the ideal time to find \mathcal{R} , as any finite projection of the inaccurately measured M^* onto N will produce very large errors in E_{M^*} . Indeed, a deflection of E_M relative to its average value is observed near 22:34:02 UT, where E_N is sharply peaked. For comparison, the B_N reversal occurs at 22:34:02.1–22:34:02.4 UT in most coordinate systems. The time we have used to find E_M , 22:34:03–22:34:04 UT, also has very weak magnetic fields, meaning that the $\vec{V} \times \vec{B}$ offset in the spacecraft-frame electric field from the relative motion of the X-line is minimized. For our simple picture of 2-D, laminar, and steady state reconnection, the reconnection electric field should be more-or-less constant in time and space, at least in the highly local region surrounding the EDR, while E_L and E_N are not constant and vary considerably. Therefore, we assume that a quality measurement of E_M should be one that deviates minimally from its average value. We also compare our measurements of \mathcal{R} with those of Torbert et al. (2018) and N18. Torbert et al. (2018) determined that the aspect ratio of the diffusion region was between 0.1 and 0.2. N18 determined that the opening angle of the separatrix was $\sim 12.5^\circ$, which corresponds to a normalized reconnection rate of $\mathcal{R} \approx 0.18$. These normalized reconnection rate measurements did not depend on either the magnitude of E_M or E_b , though they are not without their own sources of error. Lastly, N18 also noted that the reconnection rate of their simulation was also ~ 0.17 – 0.186 , which they determined by analyzing the separatrix opening angle and normalized reconnection electric field strength with the virtual probe data (see sections 4.1, 4.2, and Figure 9 of N18 for more details on the simulated reconnection rates).

Our 14 estimates of \mathcal{R} are shown in Figure 5. Figure 5a shows the values of \mathcal{R} measured by MMS-3, which was closer to the current sheet center than MMS-1. The reconnection rate measured by MMS-1 is shown in Figure 5b. There is a fair amount of scatter in \mathcal{R} from one coordinate system to another. For some coordinate systems, \mathcal{R} measured by MMS-3 also differs significantly from MMS-1. While the reconnection electric field should be more-or-less constant, this is not the case for the normal electric field, which is, on average, 4 times stronger for MMS-1 than MMS-3 during 22:34:03–22:34:04 UT (see Figure 1i). If the M axis is measured incorrectly as M^* , where M^* has a finite projection onto N , then we would expect significant differences in the measured reconnection rate between MMS-1 and MMS-3. Some of the differences between the values of E_M obtained by MMS-1 and MMS-3 data may also be explained by differences in the calibration of the two probes. However, given that the two values of E_M are nearly the same for some of the more reliable coordinate systems (e.g., MVA- v_e , MVA- E , and MDD-B/MVA- v_e), the intercalibration of the probes is

the blue (E_M in the X-line frame of Torbert et al., 2018, assuming a tailward X-line velocity of 150 km/s) and green (tailward X-line velocity of 300 km/s, which corresponds to a 100% error in the X-line frame of Torbert et al., 2018) crosses in Figures 5a and 5b. Given an average value of $\langle B_N \rangle \approx 0.5\text{--}0.7$ nT in the period when E_M is calculated, even such a large 100% uncertainty in the X-line velocity (150–300 km/s) only corresponds to a $\sim 2\text{--}4\%$ error in the reconnection rate for $\langle E_M \rangle \approx 3$ mV/m.

When only MMS-3 data are considered, there is an apparent consensus between the reconnection rates in the coordinate systems determined by (1) applying MVA- v_e to the electron jet reversal, (2) applying MVA- E to the EDR, (3) applying MFR to the EDR, and (4) a hybrid of MDD- B and MVA- v_e . Using MMS-3 data, the reconnection rates in these four coordinate systems are, respectively, 0.16, 0.16, 0.15, and 0.16. However, the reconnection rates determined using MMS-1 data from the same interval in the same four coordinate systems are, respectively, 13%, 26%, 38%, and 23% larger than for MMS-3. It is possible to use the correlation between E_{M*} and E_{N*} to obtain error bars for \mathcal{R} if they are caused by errors of the form $E_{M*} = \sin(\theta_{NM*})E_M + \cos(\theta_{NM*})E_N$. In this case, the errors can be reduced to $E_{M*} \approx E_M + \theta_{NM*}E_{N*}$ using the approximations that $\theta_{NM*} \ll 1$ and $E_M^2 \ll E_N^2$. Since both E_{M*} and E_{N*} are known quantities (the values of E_M and E_N in any imprecise coordinate system), the values of E_M and θ_{NM*} can be approximated by fitting a linear function to E_{N*} versus E_{M*} .

Fit lines of the type $E_{M*} = E_M + \theta_{NM*}E_{N*}$ are shown in Figures 5c and 5d for the GSW and MVA- v_e coordinate systems, respectively. Unsurprisingly, we find evidence that the M direction defined by the Y_{GSW} axis is nonorthogonal with N , as shown by the strong correlation between E_{M*} and E_{N*} . The form of the fit line can be rearranged as $\Delta E_M \equiv |E_{M*} - E_M|/E_M = |\theta_{NM*}E_{N*}|/E_M$ such that the relative error in E_M can be expressed by θ_{NM*} as a percentage of E_N . Given the maximum value of E_{N*} , which is observed to be roughly 10 times as large as E_M at the B_N reversal (see Figure 4), even the small error angle of $\theta_{NM*} = 1.3^\circ$ shown in Figure 5d corresponds to an error of $\sim 20\%$. For GSW, which had $\theta_{NM*} = 21^\circ$, a $\sim 350\%$ error would be expected if E_M was measured during the period of largest E_N . The values of θ_{NM*} for all 14 coordinate systems are shown in Figure 5e. Unsurprisingly, the value of θ_{NM*} is small for MVA- E , which defines M^* as the direction of minimum electric field variance.

The values of E_M determined by this linear regression correction are shown in Figure 5f. The four coordinate systems mentioned previously (MVA- v_e applied to the electron jet reversal interval, MVA- E applied to the EDR current sheet crossing interval, MFR applied to same interval, and a hybrid of MDD- B and MVA- v_e) have nearly identical values of E_M/E_b equal to 0.176, 0.184, 0.186, and 0.176, respectively, which have 2σ errors of $\sim 10\text{--}15\%$. Note that this correction does not account for all sources of error related to the selection of coordinates, as (1) errors due to the nonorthogonality of L and M^* can also significantly affect the reconnection rate in a similar manner to our previous approximation with $\theta_{NM*}E_{N*}$ and (2) most of the approximations described above do not hold when multiple rotations about different axes are needed to account for finite projections of M^* onto both N and L . Given that this θ_{NM*} correction does not noticeably affect the reconnection rates determined with MDD- B , yet the normal direction determined from MDD- B is separated by nearly 9° from the MVA- v_e normal and E_{M*} and E_{L*} are not very well correlated, it is likely that correcting the MDD- B reconnection rate would require more than our simple approximate linear determination of a single error angle.

4. Finding LMN and \mathcal{R} With Virtual Data

Now we estimate the errors in the measured coordinate axes and \mathcal{R} from the virtual MMS data described in section 2.4 and N18. We focus on MVA- v_e and MDD- B . Ultimately, our goal is to make the virtual data as MMS like as possible so these errors are realistic. However, since we do not know, for instance, how 3-D and time-dependent effects are manifested in the MMS data (or the degree to which they are present), the errors we estimate here will inevitably be conservative. However, as was discussed in sections 2 and 3.2, if 3-D and time-dependent effects are indeed manifested in the MMS data, they do not seem to cause any major differences between the actual and virtual MMS data.

First, we consider the errors in the MVA- v_e coordinate system. Assuming that the direction of v_e is correct on average, the only source of measurement error should be the noise. We have estimated that the noise in v_e is around 2,500 km/s, which is 14% of the largest value of $v_{eM} \approx 15,000$ km/s observed by MMS-3 in the EDR. Also, in the virtual MMS-3 data (Figure 1o), v_{eN} varies over the electron jet reversal period, though MVA- v_e defines the N direction as the direction of minimum variance. Lastly, we reiterate that the separation between the L and M eigenvalues was larger for MMS-3 than it was for the other three spacecraft. In total, we conclude that the most likely candidates for sources of error in MVA- v_e are noise and incorrect assumptions

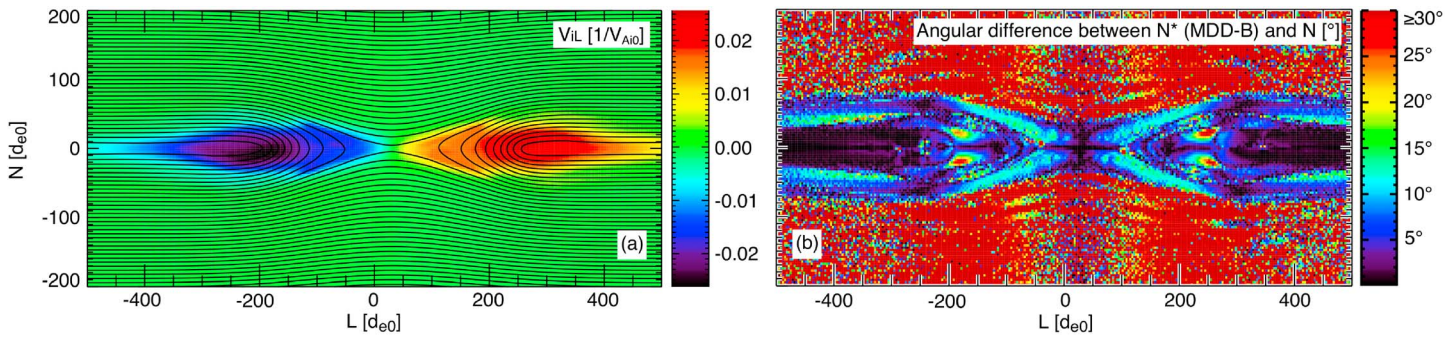


Figure 7. (b) The difference between the maximum directional derivative of \vec{B} direction and the current sheet normal when MDD-B is applied to every cell of the simulation near the diffusion region. (a) For scale, the ion bulk velocity in the jet direction. MDD = maximum directional derivative.

about the configuration of the electron velocity in LMN , which may be worsened with distance to the current sheet center.

Figure 6 shows the error in the coordinate axes, L^* , M^* , and N^* , as well as \mathcal{R}^* , which were determined by applying MVA to the noisy virtual v_e . As in section 1, we use the asterisk to mark quantities that are known to be incorrect. For example, L^* may be defined by the maximum variance direction of v_e ; however, it is known to be different from the true L axis of the simulation. The total angular error in L^* is referred to as $\theta_{LL^*} \equiv \cos^{-1}(\hat{L} \cdot \hat{L}^*)$, being the angle between the measured L^* axis and the true L axis. To find the error terms that are shown in Figure 6, we have done the following: (1) we averaged v_e along the virtual probe path in order to obtain a realistic number of data points (~ 70) within the electron jet reversal interval, such that the resolution of the virtual data is comparable to the resolution of fast plasma investigation. (2) We introduced noise to v_e using a random number generator. The most probable value for the random noise is 0 km/s, and the standard deviation of the noise was chosen to be $\pm 14\%$ of the largest value of v_e along the path of the virtual MMS-3 (see red curve in Figure 1p). (3) We adjusted the interval to maximize the eigenvalue separation. (4) We applied MVA to the noisy v_e data, reiterating the process 10^6 times to ensure statistically meaningful results. (5) We reiterated this process for different virtual probe paths, which were identical in shape to the path of the virtual MMS-3 but shifted away from the current sheet center along N (similar to the orbits of the virtual MMS-1, 2, and 4, as is shown in Figure 1p). The crosses (X) in Figures 6a–6d indicate the errors in L^* , M^* , N^* , and \mathcal{R}^* (respectively) that were averaged over all 10^6 iterations of MVA- v_e . The two dashed curved in Figures 6a–6c are the average error plus or minus a standard deviation. The error in the reconnection rate, which is shown in Figure 6d, is the difference between the average E_{M^*} (E in the direction of the measured M^* axis) and the actual average E_M . The red-shaded area indicates the region where the virtual probe path has been moved away from the current sheet center by a distance greater than the size of the tetrahedron. While our original virtual probe path may be imperfect, any errors in the N location of the virtual probe are likely well within the white region. The data along the orbits in the red-shaded region (which are identical in shape to the orbit of virtual MMS-3, but shifted southward, away from the current sheet, by ΔN) differ considerably from the observations of MMS.

First, we note that the errors in the coordinate axes due to the noise in v_e are not very large. Nevertheless, the total errors in L^* , M^* , and N^* are considerable even for the lowest-error scenario of virtual MMS-3 ($\Delta N = 0$), being approximately $5^\circ \pm 2^\circ$ for θ_{LL^*} and θ_{MM^*} and $4^\circ \pm 2^\circ$ for θ_{NN^*} . θ_{LL^*} and θ_{MM^*} increase rapidly with the distance from the current sheet center ΔN , as expected, nearly doubling from the orbit of MMS-3 ($\Delta N = 0$) to the orbits of MMS-2 and 4 ($|\Delta N| = 0.43 d_{e0}$). The error terms θ_{LL^*} and θ_{MM^*} exceed 20° in the red-shaded region at $\Delta N \approx -0.7 d_{e0}$. In contrast, θ_{NN^*} is somewhat stable over the displayed range of ΔN , though it begins to increase around $\Delta N \leq -0.8 d_{e0}$ when the noisy variance of v_{eN} approaches the magnitude of the total (physical and noisy) variance of v_{eL} and v_{eM} . For these virtual paths, the probes are far enough away from the electron current and jet layer that the variations in v_{eL} and v_{eM} are comparable in magnitude to those of v_{eN} . The small standard deviations of θ_{LL^*} , θ_{MM^*} , and θ_{NN^*} relative to their mean values indicate that the largest source of error is the incorrect assumption that the eigenvectors of MVA- v_e are identical to the LMN coordinate axes. When MVA is applied to the noiseless virtual v_e data, there is no change to the average θ_{LL^*} for small $\Delta N \geq -0.5 d_{e0}$, while the average values of θ_{MM^*} and θ_{NN^*} are both reduced by $\sim 1-2^\circ$.

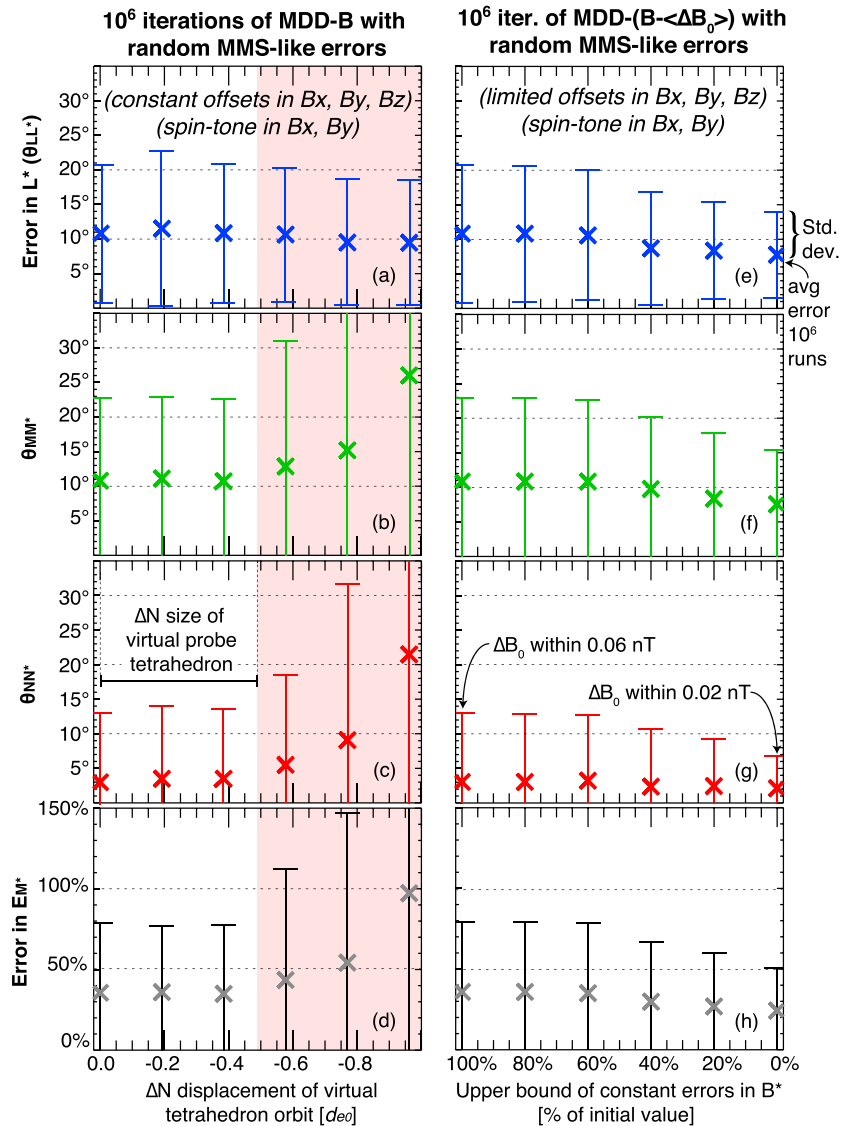


Figure 8. The errors in (a, e) L^* , (b, f) M^* , (c, g) N^* , and (d, h) the reconnection rate when MDD-B is applied to four-point virtual magnetic field data with added MMS-like offsets. In (a)–(d), the magnetic field data offsets are within 0.06 nT and the distance of the virtual tetrahedron orbit from the current sheet center is varied from the initial position determined by N18. In (e)–(h), only the virtual tetrahedron orbit from N18 is used, but the upper limits of the constant-in-time-and-space offsets, which are added to the virtual \vec{B} data, are reduced from 0.06 nT (constant offsets of ≤ 0.05 nT and spin tone offsets of ≤ 0.02 nT) to 0.02 nT (no constant offsets and spin tone offsets of ≤ 0.02 nT).

The error in the reconnection rate (Figure 6d) is moderate for even the *best case scenario* of $\Delta N = 0$ and extreme for the *worst case scenario* of $\Delta N \leq -2 d_{e0}$ away from the current sheet center, where $20\% \pm 20\% \leq E_{M^*} \leq 80\% \pm 60\%$. The noise in v_e can influence E_{M^*} considerably in some cases, as the standard deviation of E_{M^*} over the 10^6 iterations of MVA- v_e is comparable to the mean. This is not unexpected, as we have already mentioned that (1) a finite projection of M^* onto N will be more likely to create errors in E_{M^*} than a finite projection of M^* onto L , given that E_N is typically much stronger than E_L and E_M and (2) the noise affects θ_{MM^*} and θ_{NN^*} more than θ_{LL^*} . This point is demonstrated in Figure 6e, which shows $|90^\circ - \theta_{LM^*}|$ (the degree to which M^* is nonorthogonal with L) on the horizontal axis, $|90^\circ - \theta_{NM^*}|$ on the vertical axis, and the average value of E_{M^*} per bin as the third dimension (color bar). As is evident, E_{M^*} is much larger when M^* has a finite projection onto N than it is when M^* has the same sized projection onto L . In the previous section, we estimated $\theta_{NN^*} \approx 1.3^\circ$, which corresponds to a relatively small error in E_{M^*} of ~ 10 – 15% (Figure 6d).

Next we consider MDD- B . Unlike MVA- v_e , MDD- B can be applied to every point in space without integrating or averaging over a flight path, as has been done in Figure 7b. Without accounting for MMS-like errors, MDD- B is able to identify the L and N directions almost exactly for all points near the EDR and central current sheet. The errors in the L^* and N^* direction are large near the separatrices and jet braking regions, where real currents cause strong gradients in \vec{B} that are not aligned with N . There are also large errors in the inflow region, where the noisy spatial fluctuations in \vec{B} are comparable to the very small physical gradients. The M direction can be identified perfectly at all points in space since it is exactly invariant in our 2-D simulation. We also find very small errors in L^* , M^* , and N^* when MDD- B is applied to the virtual tetrahedron data using the linear gradient technique (not pictured). The errors introduced by the linear gradient assumption are $\sim 1-2^\circ$ for L^* and N^* and $\leq 0.5^\circ$ for M^* . Given that the virtual tetrahedron is similar to the actual MMS tetrahedron in terms of size and regularity, these errors from nonlinear gradients should be directly comparable to those that we expect from MMS if the magnetic field data were perfectly calibrated.

Given that the errors associated with the assumptions of MDD- B and the linear gradient technique are small, we expect the dominant source of error (excluding possible effects from time evolution and 3-D structure) to be related to the intercalibration of the magnetic field data rather than noise, as the errors in MDD- B caused by noise were shown to be small in Denton et al. (2012). We make the virtual data more MMS-like by adding very small and semirandom errors to the four-virtual-probe magnetic field data, applying MDD- B , then reiterating, much like we did previously for MVA- v_e . The errors in the virtual spin-axis ($\sim N$) and virtual-spin-plane ($\sim L$ and $\sim M$) components of \vec{B} are treated differently. The four-virtual-probe spin axis errors are added as random constant offsets, which are between +0.05 and -0.05 nT (i.e., $\sim \pm 0.0042B_b$). Smaller random and constant offsets between +0.002 and -0.002 nT were added to B_L and B_M . Spin-tone-like offsets were also added to B_L and B_M with 90° phase differences. The amplitudes of the spin tones were fixed at 0.02 nT, but the differences between the phases of the virtual probes were chosen at random. In total, the absolute error assigned to any one of the virtual \vec{B} measurements was no more than 0.06 nT, which is well below the 0.1-nT reported accuracy of fluxgate magnetometers but comparable to the interprobe differences in \vec{B} observed during a quiet interval following the 11 July 2017 event.

The error terms θ_{LL^*} , θ_{MM^*} , θ_{NN^*} , and E_{M^*} for MDD- B are shown in Figures 8a–8d. The horizontal axes of Figures 8a–8d are similar to the horizontal axes of Figures 6a–6d, though in Figures 8a–8d they represent the displacement of the entire virtual tetrahedron from its initial position, rather than the displacement of the virtual MMS-3. We find that θ_{LL^*} , θ_{MM^*} , θ_{NN^*} , and E_{M^*} are quite large, even within $\Delta N \geq -0.8 d_{e0}$. Unlike for MVA- v_e , θ_{LL^*} , θ_{MM^*} , θ_{NN^*} , and E_{M^*} do not change significantly within $\Delta N \geq -0.5 d_{e0}$. Also, unlike MVA- v_e , the errors in the coordinate axes and reconnection rate are almost entirely due to measurement errors. This point is clearly illustrated by the case of θ_{MM^*} , which is shown in Figure 8b. Even though the derivative of \vec{B} is set to be exactly 0 in the M direction, the average error in M^* is at least 10° ($\pm 12^\circ$). Similar values of θ_{LL^*} are observed, which remains more or less constant as a function of ΔN . The average errors in the N^* direction are roughly 3 times smaller than the average θ_{LL^*} and θ_{MM^*} for small ΔN , but both θ_{NN^*} and θ_{MM^*} begin to rapidly increase at large ΔN .

The (likely conservative) errors shown in Figure 8d demonstrate that the errors in the reconnection rate can be considerable when M is determined using the MDD- B technique. This is not unexpected, as the eigenvalue of $\nabla \vec{B}(\nabla \vec{B})^T$ associated with the invariant direction is 0, meaning that it is the direction that is most easily corrupted by error (Denton et al., 2010, 2012). In contrast, the normal direction, which is the direction that corresponds to the largest eigenvalue of $\nabla \vec{B}(\nabla \vec{B})^T$, will be the most robust direction. This is consistent with the fact that $\theta_{NN^*} < \theta_{LL^*} < \theta_{MM^*}$ was observed for orbits near the central current sheet (white area in Figures 8a–8d).

For Figures 8e–8h we consider a reduction in the constant offsets in B_N but no reduction in the spin tone offsets in B_L and B_M . When the constant \vec{B} offsets are removed, the errors in the coordinate axes and reconnection rate are reduced, as is shown in Figures 8e–8h. This is similar to how the MDD- $(B - \Delta B_0)$ coordinate system was determined (section 3.1.5). The average errors in the coordinate axes and reconnection rate are reduced by 25–35% when the largest possible random magnetic field errors are reduced from 0.06 to 0.02 nT. Compared to the background field of $B_b = 12$ nT, these thresholds represent a fractional sensitivity of 0.5% and $< 0.2\%$. Compared to the *worst case scenario*, where the errors in the magnetic field are exactly 0.06 nT (rather than within 0.06 nT), the average values of θ_{LL^*} and θ_{MM^*} ($= 35^\circ$) and E_{M^*} ($= 116\%$) are reduced by nearly 80% (not pictured). As was suggested previously, Figures 8e–8h show that the overall errors in θ_{LL^*} , θ_{MM^*} , θ_{NN^*} , and E_{M^*} are somewhat but not entirely reduced with this technique, since the removal of the spin tone would

require time-dependent calibration curves. It is not clear how precisely we were able to identify and remove the constant offsets from the MMS data before finding the adjusted MDD- $(B - \Delta B_0)$ coordinate system. Even for the best case scenario, for which no constant offsets have been added, the average values of θ_{LL^*} , θ_{MM^*} , and E_{M^*} are still larger than those of MVA- v_e . The average values of θ_{NN^*} , conversely, are typically for MDD- B and MDD- $(B - \Delta B_0)$ than they are for MVA- v_e .

5. Summary and Conclusions

We have investigated the accuracy with which we can find the LMN boundary normal coordinate system and reconnection rate E_M of the MMS magnetotail EDR event on 11 July 2017 at 22:34 UT. Overall, our results indicate that the reconnection electric field was within $2.5 \leq E_M \leq 4$ mV/m, which corresponds to a normalized reconnection rate of $0.14 \leq \mathcal{R} \leq 0.22$ (assuming the normalization parameter is $E_b = 18.12$ mV/m). We concluded that the most reliable coordinate systems are determined for this event by (1) applying MVA- v_e to the probe nearest the neutral sheet, where the electron jet reversal is most pronounced, (2) applying MDD- B after approximating and removing the constant (in time) offsets in the four-point measurements of \vec{B} , (3) applying MFR to the region near the EDR where the X-line velocity appears to be constant in time, and (4) using a hybrid approach, for example, where MVA- v_e was used to determine L , MDD- B is used to determine N perpendicular to L , and the third coordinate axis completes the right-handed system. However, each technique had its own sources of error, implying that one technique may not be the best for finding all coordinate axes for all events. We found that the correlation between the reconnection rates determined with these five coordinate systems was strongest for the spacecraft nearest the neutral sheet (MMS-3), likely since E_N —and therefore, the projections of E_N onto the imprecisely measured M axes—are reduced near the neutral sheet. Lastly, we attempted to optimize each coordinate system by determining and removing linear correlations between E_N and E_M . In these optimized coordinates, we found that the reconnection rate was likely $E_M = 3.2 \pm 0.6$ mV/m and $\mathcal{R} = 0.18 \pm 0.035$.

We also compared the accuracy of the MVA- v_e and MDD- B techniques using virtual MMS data from the EDR of a 2.5-D PIC simulation of this 11 July 2017 event, which was performed in our companion paper, Nakamura et al. (2018, referred to as N18 throughout this paper). We found that the largest source of error for the MVA- v_e technique was the incorrect assumption that the principle variance axes of v_e were identical to the principle (LMN) axes of the EDR. Poor separation of the maximum and intermediate variance directions lead to moderate errors in the measured L and M axes, which grew rapidly as a function of the distance between the virtual probe path and the center of the current sheet. Errors in v_e , which are assumed to come predominantly from noise due to low counts, did not have a dramatic effect on the quality of the coordinate system and reconnection rate. When determined with MVA- v_e , the error in the simulated reconnection rate was moderate (~ 20 – 40%). This error was considerably smaller when the M and N axes were well separated, which was most often the case. The accuracy of these techniques differed when the trajectory of the virtual probes through the EDR was altered, especially for MVA- v_e .

Large errors in the L and M coordinate axes (~ 10 – 20°) and reconnection rate (~ 50 – 80%) were found when MDD- B was applied to the virtual tetrahedron data and MMS-like errors were introduced to \vec{B} . These errors in \vec{B} were expected to result from small errors in the intercalibration of the magnetometers. When the constant offsets in \vec{B} were not considered, and only a varying spin tone was added, the errors in the L and M coordinate axes (~ 8 – 15°) were somewhat reduced and the errors in the reconnection rate (~ 25 – 50%) were dramatically reduced. This was likely due to the reduction in θ_{NM^*} , the nonorthogonality of the N axis and measured M^* axis. Unlike MVA- v_e , the errors in the magnetic field data were likely the only source of error for MDD- B , as the errors due to (1) the underlying assumption that the eigenvectors of $\nabla \vec{B}(\nabla \vec{B})^T$ are equivalent to the LMN coordinate axes and (2) nonlinear gradients of \vec{B} within the virtual tetrahedron were negligible.

Lastly, we reiterate that we have only focused on one of the sources of error in \mathcal{R} , which comes from the inaccurate determination of M . Our measurements of the normalized reconnection rate were based on $E_b = 18.12$ mV/m, though different but also reasonable selections of upstream parameters (see section 2.2) could have been made such that E_b was 30% larger or smaller than our chosen value. Nominally, the accuracy of the perpendicular electric field is reported as 0.5 mV/m, which is one fifth of our measured reconnection electric field. The electric field data we have used were specially calibrated for this event (see Torbert et al., 2018), so it is not clear whether this reported accuracy is reasonable. However, all of these sources of error coexist and compound one another in a manner that has not been accounted for in this study. Given the

Table A1
LMN Coordinate System Axes in GSE

[#]	Method	$[L_x, L_y, L_z]$	$[M_x, M_y, M_z]$	$[N_x, N_y, N_z]$
1	GSW	[0.9986, −0.0521, 0.0052]	[0.0523, 0.9980, 0.0362]	[−0.0019, −0.0361, 0.9993]
2	Modeled N.S.	[0.9986, −0.0521, 0.0052]	[0.0523, 0.9966, −0.0633]	[−0.0019, 0.0635, 0.9980]
3	MVA-B (excluding RX interval)	[0.9935, −0.1137, −0.0107]	[0.1008, 0.9168, −0.3865]	[0.0537, 0.3829, 0.9222]
4	MVA-B (only RX interval)	[0.9984, −0.0454, 0.0334]	[0.0562, 0.8489, −0.5256]	[−0.0045, 0.5266, 0.8501]
5	MVA-E (long C.S. crossing)	[0.9352, −0.3495, 0.0566]	[0.3497, 0.8865, −0.3030]	[0.0557, 0.3032, 0.9513]
6	MVA-E (EDR interval)	[0.9750, −0.2223, 0.0017]	[0.2105, 0.9208, −0.3284]	[0.0715, 0.3205, 0.9445]
7	MVA- v_i	[0.9677, −0.2476, −0.0482]	[0.2477, 0.9688, −0.0038]	[0.0476, −0.0083, 0.9988]
8	MVA- v_e	[0.9482, −0.2551, −0.1893]	[0.1749, 0.9168, −0.3591]	[0.2651, 0.3074, 0.9139]
9	MFR	[0.9754, −0.2131, 0.0568]	[0.2202, 0.9286, −0.2986]	[0.0109, 0.3038, 0.9527]
10	MDD-B (one interval)	[0.8778, 0.4194, −0.2315]	[−0.4697, 0.8485, −0.2438]	[0.0942, 0.3227, 0.9418]
11	MDD-B (two intervals)	[0.9451, 0.2673, −0.1866]	[−0.3139, 0.9011, −0.2990]	[0.0947, 0.3225, 0.9418]
12	MDD- $(B - \langle \Delta B \rangle_0)$	[0.9858, 0.0856, −0.1443]	[−0.1290, 0.9367, −0.3256]	[0.1073, 0.3395, 0.9341]
13	Hybrid MDD-B / Max J_M (Torbert et al., 2018)	[0.971, −0.216, −0.106]	[0.234, 0.948, −0.215]	[0.054, 0.233, 0.971]
14	Hybrid MDD-B / MVA- v_e	[0.9482, −0.2551, −0.1893]	[0.1818, 0.9245, −0.3350]	[0.2604, 0.2832, 0.9230]

Note. GSW = solar-wind-aberrated geocentric solar magnetospheric; MVA = minimum variance analysis; EDR = electron diffusion region; MFR = minimization of Faraday residue; MDD = maximum directional derivative; C.S. = Current Sheet; N.S. = Neutral Sheet; GSE = Geocentric Solar Ecliptic.

similarity between our measurements of the reconnection rate and those of Torbert et al. (2018) and N18, it is also possible that ours are estimates that are close to the real value \mathcal{R} . Regardless, our results indicate that one should be cautious if comparing similar reconnection rates between two or more events, since the reconnection rate for any single event can have very large error bars, which may not be easily estimated.

Appendix A: Coordinate System Definitions

The coordinate systems in Table A1 are determined using the techniques outlined in section 3. The leftmost column refers to the order in which each coordinate system appeared in the enumerated list of section 3.1.6.

Acknowledgments

We would like to thank everyone who contributed to the success of the Magnetospheric Multiscale (MMS) mission. We would like to thank the Scientist in the Loop (SITL), R. E. Ergun, and the SITL on deck, M. Akhavan-Tafti, for selecting this event as one in which high-resolution MMS data are available. This work was done in collaboration with the ISSI group "Plasma Heating and Acceleration by Collisionless Magnetic Reconnection." MMS data were obtained from the Science Data Center (SDC) at <https://lasp.colorado.edu/mms/sdc/>. The Space Physics Environment Data Analysis Software (SPEDAS) package was used to process the MMS data. K. J. Genestreti was supported by the Austrian FFG project 847969. R. Nakamura and T. K. M. Nakamura were supported by the Austrian FWF grant I2016-N20. R. E. Denton was supported by NASA grant NNX14AC38G. For the simulation data used in this research, T. K. M. Nakamura acknowledges PRACE for awarding the access to MareNostrum at Barcelona Supercomputing Center (BSC), Spain.

References

- Arridge, C. S., Eastwood, J. P., Jackman, C. M., Poh, G.-K., Slavin, J. A., Thomsen, M. F., et al. (2016). Cassini in situ observations of long-duration magnetic reconnection in Saturn's magnetotail. *Nature Physics*, 12, 268–271. <https://doi.org/10.1038/nphys3565>
- Bowers, K. J., Albright, B. J., Yin, L., Bergen, B., & Kwan, T. J. T. (2008). Ultrahigh performance three-dimensional electromagnetic relativistic kinetic plasma simulation. *Physics of Plasmas*, 15(5), 55703. <https://doi.org/10.1063/1.2840133>
- Bowers, K. J., Albright, B. J., Yin, L., Daughton, W., Roytershteyn, V., Bergen, B., & Kwan, T. J. T. (2009). Advances in petascale kinetic plasma simulation with VPIC and Roadrunner. *Journal of Physics Conference Series*, 180, 12055. <https://doi.org/10.1088/1742-6596/180/1/012055>
- Chanteur, G. (1998). Spatial interpolation for four spacecraft: Theory. In G. Paschmann & P. W. Daly (Eds.), *Analysis Methods for Multi-Spacecraft Data* (chap. 14, pp. 349–370). Bern, Switzerland: International Space Science Institute.
- Che, H. (2017). How anomalous resistivity accelerates magnetic reconnection. *Physics of Plasmas*, 24(8), 82115. <https://doi.org/10.1063/1.5000071>
- Chen, L.-J., Hesse, M., Wang, S., Gershman, D., Ergun, R. E., Burch, J., et al. (2017). Electron diffusion region during magnetopause reconnection with an intermediate guide field: Magnetospheric Multiscale observations. *Journal of Geophysical Research: Space Physics*, 122, 5235–5246. <https://doi.org/10.1002/2017JA024004>
- Denton, R. E., Sonnerup, B. U. Ö., Birn, J., Teh, W.-L., Drake, J. F., Swisdak, M., et al. (2010). Test of methods to infer the magnetic reconnection geometry from spacecraft data. *Journal of Geophysical Research*, 115, A10242. <https://doi.org/10.1029/2010JA015420>
- Denton, R. E., Sonnerup, B. U. Ö., Russell, C. T., Hasegawa, H., Strangeway, R. J., Giles, B. L., et al. (2018). Determining L-M-N current sheet coordinates at the magnetopause from Magnetospheric Multiscale data. *Journal of Geophysical Research: Space Physics*, 123, 2274–2295. <https://doi.org/10.1029/2005JA011538>
- Denton, R. E., Sonnerup, B. U. Ö., Swisdak, M., Birn, J., Drake, J. F., & Hesse, M. (2012). Test of Shi et al. method to infer the magnetic reconnection geometry from spacecraft data: MHD simulation with guide field and antiparallel kinetic simulation. *Journal of Geophysical Research*, 117, A09201. <https://doi.org/10.1029/2012JA017877>
- Egedal, J., Fox, W., Katz, N., Porkolab, M., Reim, K., & Zhang, E. (2007). Laboratory observations of spontaneous magnetic reconnection. *Physical Review Letters*, 98, 15003. <https://doi.org/10.1103/PhysRevLett.98.015003>
- Ergun, R. E., Tucker, S., Westfall, J., Goodrich, K. A., Malaspina, D. M., Summers, D., et al. (2016). The axial double probe and fields signal processing for the MMS mission. *Space Science Reviews*, 199, 167–188. <https://doi.org/10.1007/s11214-014-0115-x>
- Fairfield, D. H. (1980). A statistical determination of the shape and position of the geomagnetic neutral sheet. *Journal of Geophysical Research*, 85, 775–780. <https://doi.org/10.1029/JA085IA02p00775>

- Fuselier, S. A., & Lewis, W. S. (2011). Properties of near-Earth magnetic reconnection from in-situ observations. *Space Science Reviews*, 160, 95–121. <https://doi.org/10.1007/s11214-011-9820-x>
- Fuselier, S. A., Lewis, W. S., Schiff, C., Ergun, R., Burch, J. L., Petrinesc, S. M., & Trattner, K. J. (2016). Magnetospheric Multiscale science mission profile and operations. *Space Science Reviews*, 199, 77–103. <https://doi.org/10.1007/s11214-014-0087-x>
- Fuselier, S. A., Trattner, K. J., Petrinesc, S. M., Owen, C. J., & Rème, H. (2005). Computing the reconnection rate at the Earth's magnetopause using two spacecraft observations. *Journal of Geophysical Research*, 110, A06212. <https://doi.org/10.1029/2004JA010805>
- Genestreti, K. J., Fuselier, S. A., Goldstein, J., Nagai, T., & Eastwood, J. P. (2014). The location and rate of occurrence of near-Earth magnetotail reconnection as observed by Cluster and Geotail. *Journal of Atmospheric and Solar-Terrestrial Physics*, 121, 98–109. <https://doi.org/10.1016/j.jastp.2014.10.005>
- Haaland, S. E., Sonnerup, B. U. O., Dunlop, M. W., Balogh, A., Georgescu, E., Hasegawa, H., et al. (2004). Four-spacecraft determination of magnetopause orientation, motion and thickness: Comparison with results from single-spacecraft methods. *Annales Geophysicae*, 22(4), 1347–1365. <https://doi.org/10.5194/angeo-22-1347-2004>
- Khrabrov, A. V., & Sonnerup, B. U. O. (1998). Orientation and motion of current layers: Minimization of the Faraday residue. *Geophysical Research Letters*, 25, 2373–2376. <https://doi.org/10.1029/98GL51784>
- Lindqvist, P.-A., Olsson, G., Torbert, R. B., King, B., Granoff, M., Rau, D., et al. (2016). The spin-plane double probe electric field instrument for MMS. *Space Science Reviews*, 199, 137–165. <https://doi.org/10.1007/s11214-014-0116-9>
- Liu, Y.-H., Hesse, M., Guo, F., Daughton, W., Li, H., Cassak, P. A., & Shay, M. A. (2017). Why does steady-state magnetic reconnection have a maximum local rate of order 0.1? *Physical Review Letters*, 118(085), 101. <https://doi.org/10.1103/PhysRevLett.118.085101>
- Liu, Y. H., Mouikis, C. G., Kistler, L. M., Wang, S., Roytershteyn, V., & Karimabadi, H. (2015). The heavy ion diffusion region in magnetic reconnection in the Earth's magnetotail. *Journal of Geophysical Research: Space Physics*, 120, 3535–3551. <https://doi.org/10.1002/2015JA020982>
- Mozer, F. S., Bale, S. D., & Phan, T. D. (2002). Evidence of diffusion regions at a subsolar magnetopause crossing. *Physical Review Letters*, 89(1), 15002. <https://doi.org/10.1103/PhysRevLett.89.015002>
- Mozer, F. S., & Retinò, A. (2007). Quantitative estimates of magnetic field reconnection properties from electric and magnetic field measurements. *Journal of Geophysical Research*, 112, A10206. <https://doi.org/10.1029/2007JA012406>
- Nakamura, T. K. M., Eriksson, S., Hasegawa, H., Zenitani, S., Li, W. Y., Genestreti, K. J., et al. (2017). Mass and energy transfer across the Earth's magnetopause caused by vortex-induced reconnection. *Journal of Geophysical Research: Space Physics*, 122, 11,505–11,522. <https://doi.org/10.1002/2017JA024346>
- Nakamura, T. K. M., Genestreti, K. J., Liu, Y.-H., Nakamura, R., Teh, W.-L., Hasegawa, H., et al. (2018). Measurement of the magnetic reconnection rate in the Earth's magnetotail. *Journal of Geophysical Research: Space Physics*, 123. <https://doi.org/10.1029/2018JA025713>
- Paschmann, G., Papamastorakis, I., Baumjohann, W., Scokpe, N., Carlson, C. W., Sonnerup, B. U. O., & Lühr, H. (1986). The magnetopause for large magnetic shear—AMPTE/IRM observations. *Journal of Geophysical Research*, 91, 11,099–11,115. <https://doi.org/10.1029/JA091iA10p11099>
- Phan, T. D., Gosling, J. T., Davis, M. S., Skoug, R. M., Øieroset, M., Lin, R. P., et al. (2006). A magnetic reconnection X-line extending more than 390 Earth radii in the solar wind. *Nature*, 439, 175–178. <https://doi.org/10.1038/nature04393>
- Phan, T. D., Paschmann, G., Twitty, C., Mozer, F. S., Gosling, J. T., Eastwood, J. P., et al. (2007). Evidence for magnetic reconnection initiated in the magnetosheath. *Geophysical Research Letters*, 34, L14104. <https://doi.org/10.1029/2007GL030343>
- Pollock, C., Moore, T., Jacques, A., Burch, J., Gliese, U., Saito, Y., et al. (2016). Fast Plasma Investigation for Magnetospheric Multiscale. *Space Science Reviews*, 199, 331–406. <https://doi.org/10.1007/s11214-016-0245-4>
- Rezeau, L., Belmont, G., Manuzza, R., Aunai, N., & Dargent, J. (2018). Analyzing the magnetopause internal structure: New possibilities offered by MMS tested in a case study. *Journal of Geophysical Research: Space Physics*, 123, 227–241. <https://doi.org/10.1002/2017JA024526>
- Russell, C. T., Anderson, B. J., Baumjohann, W., Bromund, K. R., Dearborn, D., Fischer, D., et al. (2016). The Magnetospheric Multiscale magnetometers. *Space Science Reviews*, 199, 189–256. <https://doi.org/10.1007/s11214-014-0057-3>
- Shay, M. A., Phan, T. D., Haggerty, C. C., Fujimoto, M., Drake, J. F., Malakit, K., et al. (2016). Kinetic signatures of the region surrounding the X line in asymmetric (magnetopause) reconnection. *Geophysical Research Letters*, 43, 4145–4154. <https://doi.org/10.1002/2016GL069034>
- Shi, Q. Q., Shen, C., Pu, Z. Y., Dunlop, M. W., Zong, Q.-G., Zhang, H., et al. (2005). Dimensional analysis of observed structures using multipoint magnetic field measurements: Application to Cluster. *Geophysical Research Letters*, 32, L12105. <https://doi.org/10.1029/2005GL022454>
- Slavin, J. A., Acuña, M. H., Anderson, B. J., Baker, D. N., Benna, M., Boarden, S. A., et al. (2009). MESSENGER observations of magnetic reconnection in Mercury's magnetosphere. *Science*, 324, 606. <https://doi.org/10.1126/science.1172011>
- Sonnerup, B. U. O. (1987). On the stress balance in flux transfer events. *Journal of Geophysical Research*, 92, 8613–8620. <https://doi.org/10.1029/JA092iA08p08613>
- Sonnerup, B. U. O., & Cahill, L. J. Jr. (1967). Magnetopause structure and attitude from Explorer 12 observations. *Journal of Geophysical Research*, 72, 171. <https://doi.org/10.1029/JZ072i001p00171>
- Sonnerup, B. U. O., Haaland, S., Paschmann, G., Dunlop, M. W., Rème, H., & Balogh, A. (2006). Orientation and motion of a plasma discontinuity from single-spacecraft measurements: Generic residue analysis of Cluster data. *Journal of Geophysical Research*, 111, A05203. <https://doi.org/10.1029/2005JA011538>
- Sonnerup, B. U. O., & Hasegawa, H. (2005). Orientation and motion of two-dimensional structures in a space plasma. *Journal of Geophysical Research*, 110, A06208. <https://doi.org/10.1029/2004JA010853>
- Stawarz, J. E., Eastwood, J. P., Genestreti, K. J., Nakamura, R., Ergun, R. E., Burgess, D., et al. (2018). Intense electric fields and electron-scale substructure within magnetotail flux ropes as revealed by the Magnetospheric Multiscale mission. *Geophysical Research Letters*, 45, 8783–8792. <https://doi.org/10.1029/2018GL079095>
- Torbert, R. B., Burch, J. L., Phan, T. D., Hesse, M., Argall, M., Shuster, R. J., et al. (2018). Electron-scale dynamics of the diffusion region during symmetric magnetic reconnection in space. *Science*. <https://doi.org/10.1126/science.aat2998>
- Torbert, R. B., Vaith, H., Granoff, M., Widholm, M., Gaidos, J. A., Briggs, B. H., et al. (2016). The electron drift instrument for MMS. *Space Science Reviews*, 199(1), 283–305. <https://doi.org/10.1007/s11214-015-0182-7>
- Wang, S., Kistler, L. M., Mouikis, C. G., Liu, Y., & Genestreti, K. J. (2014). Hot magnetospheric O⁺ and cold ion behavior in magnetopause reconnection: Cluster observations. *Journal of Geophysical Research: Space Physics*, 119, 9601–9623. <https://doi.org/10.1002/2014JA020402>
- Wang, R., Nakamura, R., Lu, Q., Baumjohann, W., Ergun, R. E., Burch, J. L., et al. (2017). Electron-scale quadrants of the hall magnetic field observed by the Magnetospheric Multiscale spacecraft during asymmetric reconnection. *Physical Review Letters*, 118(175), 101. <https://doi.org/10.1103/PhysRevLett.118.175101>

- Wygant, J. R., Cattell, C. A., Lysak, R., Song, Y., Dombeck, J., McFadden, J., et al. (2005). Cluster observations of an intense normal component of the electric field at a thin reconnecting current sheet in the tail and its role in the shock-like acceleration of the ion fluid into the separatrix region. *Journal of Geophysical Research*, 110, A09206. <https://doi.org/10.1029/2004JA010708>
- Xiao, C. J., Pu, Z. Y., Wang, X. G., Ma, Z. W., Fu, S. Y., Phan, T. D., et al. (2007). A Cluster measurement of fast magnetic reconnection in the magnetotail. *Geophysical Research Letters*, 34, L01101. <https://doi.org/10.1029/2006GL028006>
- Zenitani, S., Hesse, M., Klimas, A., & Kuznetsova, M. (2011). New measure of the dissipation region in collisionless magnetic reconnection. *Physical Review Letters*, 106(19), 195003. <https://doi.org/10.1103/PhysRevLett.106.195003>